

Asteroseismology of *Kepler* SPB stars using TESS mission light curves can yield similarly well-constrained parameters

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ABSTRACT

The slowly pulsating B (SPB) stars are a class of variable star with masses between about 3 and 8 M_{\odot} . Their gravity-mode pulsation frequencies are sensitive to the near-core structure, which makes them useful probes of rotation and mixing in the deep stellar interior. Time series photometry, such as from the *Kepler* and TESS space telescopes, allows the extraction of their pulsation frequencies and construction of period spacing patterns. Previously, samples of slowly pulsating B stars were observed by the *Kepler* mission and underwent forward asteroseismic modelling to retrieve stellar parameters such as mass, age and core mass. However, all of these stars have since been re-observed by the ongoing TESS mission with light curves that are usually shorter and non-continuous, resulting in more difficult frequency extraction and interpretation in terms of constructing period spacing patterns. In this paper we compare the results of forward asteroseismic modelling of a sample of SPB stars using intermittent TESS light curve data to those based on long-duration *Kepler* light curves. We show how in some cases that the masses and core masses derived from only a few sectors of TESS data agree well with the 4-yr *Kepler* mission results, despite the stars having far fewer significant pulsation frequencies in their TESS light curves. However, some stars yield incompatible results, emphasising the complexities in forward asteroseismic modelling of gravity-mode pulsators with sparsely sampled or short duration TESS light curves.

Key words: asteroseismology - stars: oscillations - stars: early-type - stars: evolution - stars: rotation

1 INTRODUCTION

Asteroseismology is the study of stellar oscillations, whose frequencies are used to uncover the structure of the stellar interior (Aerts et al. 2010; Kurtz 2022). In particular, gravity modes (g modes) are sensitive to the structure near the convective core of intermediate- and high-mass main-sequence stars (Aerts 2021). The g modes in such stars are therefore useful for studying problems such as convective boundary mixing (CBM¹; Anders & Pedersen 2023), rotation and angular momentum transport (Aerts et al. 2019).

The slowly pulsating B (SPB) stars are main sequence stars between about 3 and 8 M_{\odot} , and pulsate in high-radial order g modes excited by the heat-engine mechanism (Dziembowski et al. 1993; Miglio et al. 2008). Pulsation frequencies of the same angular degree and azimuthal order, and consecutive radial order form a regular pattern in period following the asymptotic approximation (Tassoul 1980; Miglio et al. 2008). The first gravity-mode period spacing pattern in an SPB star was detected by Degroote et al. (2010) using data from the CoRoT mission (Auvergne et al. 2009). Later, light curves from the *Kepler* mission (Borucki et al. 2010) yielded a few dozen SPB stars (Pápics et al. 2015, 2017; Szewczuk et al. 2021). Subsequent forward asteroseismic modelling of the period spacing patterns determined their interior rotation rates, masses, ages and mixing properties

(Moravceji et al. 2015, 2016; Szewczuk & Daszyńska-Daszkiewicz 2018; Szewczuk et al. 2021, 2022; Michielsen et al. 2021, 2023; Bowman & Michielsen 2021; Pedersen et al. 2021; Pedersen 2022), but also constraints on their interior magnetic fields (Buysschaert et al. 2018; Lecoanet et al. 2022).

Between 2009 and 2013, the NASA *Kepler* mission (Borucki et al. 2010; Koch et al. 2010) assembled high-quality and long-duration light curves for over 200 000 stars, which were revolutionary for asteroseismology. In its nominal mission, the *Kepler* satellite observed a 115 deg² field of view in the constellations of Cygnus and Lyrae, and assembled almost uninterrupted 4-yr light curves at a cadence of 30 min and a typical photometric precision of order a few ppm. These unprecedentedly high-quality data allowed forward asteroseismic modelling of tens of thousands of pulsating red giants (e.g. Chaplin & Miglio 2013), hundreds of intermediate-mass dwarfs, such as γ Dor and SPB stars (see Aerts 2021), but also many different types of pulsators across the HR diagram (Kurtz 2022). However, the field of view of the nominal *Kepler* mission avoided massive stars (i.e. $M \gtrsim 8 M_{\odot}$), which means the highest mass stars directly observed by the *Kepler* mission were SPB stars (see Bowman 2020 for a review). A handful of massive stars were observed by the previous CoRoT mission (Auvergne et al. 2009), and the maximum duration of light curves from different campaigns of the K2 mission (Howell et al. 2014) were only 80 d, making them generally too short to resolve period spacing patterns of SPB stars (e.g. Bowman et al. 2019). This means that the paradigm shift of asteroseismol-

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¹ Also sometimes referred to as overshooting in the literature.

ogy to more massive stars had to await the ongoing TESS mission (BursSENS et al. 2023; Bowman 2023).

The NASA Transiting Exoplanet Survey Satellite (TESS) mission is an all-sky survey with a primary goal of detecting Earth-like exoplanets orbiting bright late-type stars (Ricker et al. 2015). The field of view of the TESS mission covers a region of $24 \times 96 \text{ deg}^2$ stretching from the ecliptic equator up to an ecliptic pole using four cameras. Each hemisphere is divided into 13 sectors, and each is observed for approximately 28 d. After observations for a sector have been completed, the satellite slews to the next sector’s field of view whilst maintaining an overlap near the ecliptic pole, defining a continuous viewing zone (CVZ). Since each of the four cameras has a square field of view, this means there are small regions of overlap between one sector and the next, and on average, a target is viewed for more sectors the larger its ecliptic latitude (Ricker et al. 2015). This means that the observing strategy of TESS is entirely complementary to that of the *Kepler* mission, with the former scanning the sky and providing relatively short light curves for many pulsating early-type stars, and the latter targeting a relatively small region of the sky for a long time. TESS is currently coming to the end of its second extended mission, and has provided light curves for millions of stars across the sky, including hundreds of β Cep and SPB stars (Pedersen et al. 2019; BursSENS et al. 2020), which are yet to be fully exploited.

The goal of this study is to investigate and validate the ability of using short-duration and intermittent light curves from the TESS mission in reproducing *Kepler* modelling output parameters for SPB stars using their g-mode period spacing patterns. We use a sub-sample of SPB stars studied previously by Pedersen et al. (2021) benchmarks to determine what fraction of the period spacing pattern frequencies extracted from *Kepler* data can be recovered from the currently available TESS sectors. We then use the g-mode period spacing patterns extracted from TESS data to perform forward asteroseismic modelling and establish if we recover the masses, core masses, and central hydrogen fractions of our sample, and discuss how these compare these to the results previously obtained from *Kepler* light curves.

2 METHODS AND DATA

2.1 Sample Selection

To demonstrate the efficacy of TESS for forward asteroseismic modelling of early-type stars, we first require a benchmark sample of SPB stars having undergone forward asteroseismic modelling to compare our TESS analysis with. Therefore, we have selected a subset of the 26 SPB stars studied using *Kepler* light curves by Pedersen et al. (2021), which allow us to compare stellar parameter estimations of mass, core mass, and central hydrogen (i.e. as a proxy for age of the main sequence) between the TESS and *Kepler* results. These parameters describe the structure of a star but also are related to processes such as CBM (see Aerts 2021).

As our overall goal was to determine for which stars we find the ‘correct’ stellar parameters from forward asteroseismic modelling of the TESS light curves, we needed to ensure that only stars with the most reliable results from the Pedersen et al. (2021) sample were included in our study. We therefore imposed three criteria to define our sample of SPB stars. First, we excluded stars with *Gaia* G -band magnitude fainter than 11 mag to allow for a robust TESS light curve extraction. For example, Bowman et al. (2024) discuss the difficulties in extracting TESS light curves of faint sources (i.e. $V \gtrsim 11$ mag). Second, we included only isolated stars, which we define as those

with no brighter stars or stars fainter by less than two magnitudes within 1 TESS pixel (i.e. 21 arc sec). This is to ensure that extraction of TESS light curves is not complicated for stars with high crowding and contamination, thus allowing for a fair comparison of *Kepler* and TESS. Finally, we used the maximum pulsation amplitude reported by Pedersen et al. (2021), and excluded stars with pulsation amplitudes below ~ 1 ppt. This was to ensure a sufficiently high signal-to-noise ratio (S/N) of the pulsation frequencies was achieved. This is necessary because the photometric precision of TESS light curves is worse than that of *Kepler* data, and coupled with the shorter light curves means low-amplitude pulsation modes may not be detectable with TESS. We also considered imposing a maximum relative error on mass reported by Pedersen et al. (2021), for example 30 per cent, although all stars passed this criterion.

The four SPB stars that satisfy all of our criteria span a range of pulsational properties allowing us to test how limited duration TESS light curves manifest in forward asteroseismic modelling under different conditions. We provide information of these four SPB stars in Table 1. For example, KIC 8766405 is the brightest star of the four with $G = 8.7884$ mag, whereas KIC 5941844 has the highest pulsation amplitude with ~ 10 mmag, and KIC 7760680 has the best relative precision and accuracy on its mass with it being quoted as around 2 per cent by Pedersen et al. (2021) and 3 per cent by Bowman & Michielsen (2021). Finally, KIC 4930889 is a detached binary with near-equal primary and secondary B-type components (Michielsen et al. 2023). In addition to these four well-studied SPB stars, which we refer to as the ‘good sample’, we added additional targets which only passed two of our three criteria to increase the sample size. These additional SPB stars include KIC 6352430 which is the brightest star in the Pedersen et al. (2021) sample, but has a nearby contaminating neighbour, and KIC 11360704 which has the largest number of available TESS sectors but it is quite faint with $G = 10.6179$ mag. Finally, we included KIC 3240411 and KIC 3459297, which failed the contamination and brightness criteria, respectively, but both have relatively unambiguous period spacing patterns (see Pedersen et al. 2021). Therefore, our final sample of SPB stars includes four good and four other targets, which are provided in Table 1.

2.2 TESS light curve extraction

Since the launch of the TESS mission, the overall quality and properties of available data products have greatly improved. For example, in the nominal mission (i.e. cycles 1 and 2), full-frame images (FFIs) were provided at a cadence of 30 min, but this was later improved to 10 min and subsequently 200 sec in the first and second extended missions, respectively. Whilst a cadence of 30 min is typically sufficient for studying g modes in SPB stars, such that the pulsation amplitudes are negligibly affected by the amplitude suppression function caused by smearing of the pulsation signal (see Bowman 2017), a faster cadence in the available FFI TESS data provides improved precision in the resultant frequency spectrum owing to the larger number of observations within each sector (Huber et al. 2022). Random noise caused by jitter is more effectively mitigated in more recent TESS sectors owing to improvements in NASA’s data reduction pipelines (Jenkins et al. 2016). Moreover, the number of allocated targets for 2-min cadence, and the more recently available 20-sec cadence, for light curve extraction based on NASA’s SPOC pipeline (Jenkins et al. 2016) has also increased since the nominal mission. This means through successful guest investigator (GI) proposals led by members of the community that many more early-type stars have 2-min light curves available (see e.g. Bowman et al. 2022). Therefore, for all of

Table 1. SPB stars studied in this work, with columns of KIC ID, TIC ID, Gaia DR3 ID, Gaia G -band magnitude, the amplitude of the dominant pulsation mode as measured in this work (see Appendix A), the relative percentage error on the derived stellar mass from forward asteroseismic modelling using *Kepler* data reported by Pedersen et al. (2021), and a contamination flag defined in this work. The four stars passing all of our selection criteria are listed first, whereas four additional cases with contamination issues are included for comparison purposes.

	KIC ID	TIC ID	Gaia DR3 ID	G (mag)	A_{\max} (mmag)	ΔM (%)	contamination flag
good stars	4930889	138425170	2052512437803141760	8.8247	6.16 ± 0.01	12	no
	5941844	120319633	2104032361519412992	9.1546	10.66 ± 0.01	3	no
	7760680	271047903	2078179471596942848	10.3611	7.16 ± 0.01	2	no
	8766405	272368354	2079732295556849536	8.7884	2.957 ± 0.005	8	no
other stars	3240411	137815897	2051930078899200768	10.2476	0.371 ± 0.006	20	yes
	3459297	139103795	2049135601386710144	12.4472	1.80 ± 0.01	18	yes
	6352430	121331677	2102391512214758144	7.8878	5.656 ± 0.006	5	yes
	11360704	27847920	2086818132599764224	10.6179	32.2 ± 1.1	15	yes

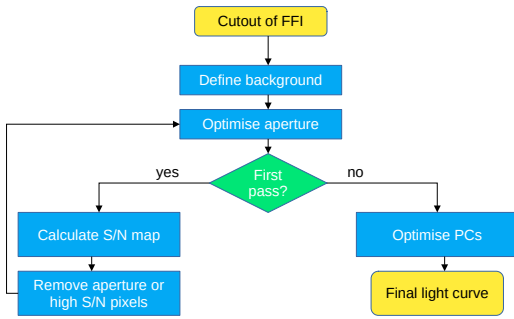


Figure 1. Flowchart describing the light curve extraction process.

the above reasons, the quality of TESS data is generally better for more recent sectors.

TESS target pixel files for each star were downloaded from the Mikulsi Archive for Space Telescopes (MAST)² public archive using the `tesscut` function (Brasseur et al. 2019; Astropy Collaboration et al. 2022) in the Python `LIGHTKURVE` software package (Lightkurve Collaboration et al. 2018). Cutouts of size 20 by 20 pixels were used. We extract light curves from TESS FFIs for our SPB targets using simple aperture photometry (SAP). We first assign pixels below the median flux as ‘background’. The aperture mask of a target in the framework of SAP is typically assigned based on flux-based significance criterion and a watershed-like algorithm applied to a median-stacked image. For studying the relatively large-amplitude pulsations in early-type stars, however, a larger aperture mask compared to that of NASA’s SPOC pipeline is usually beneficial for maximising the S/N of stellar variability (see e.g. Pápics et al. 2013, 2015; Bowman et al. 2022; Burssens et al. 2023).

In this work we have developed a new method for optimising the target aperture pixel mask of a pulsating early-type star, which uses the S/N of the dominant pulsation mode in the frequency spectrum as the metric for deciding which pixels to include or not. Our methodology is summarised in a schematic flowchart in Fig. 1, and individual steps are described in the following subsections.

2.2.1 Optimal aperture selection based on pulsation amplitude signal-to-noise ratios

The standard approach of extracting light curves is based on a flux threshold for pixels to be included in a target star’s aperture mask (or not). But this does not take into account that pulsations cause flux variability, hence a flux-based mask it is not tailored for asteroseismology of pulsations, which generally operates in the frequency domain rather than the time domain. In this work, similar to Bowman & Holdsworth (2019), we use a curve-of-growth method for optimising the size of a target’s pixel mask using the S/N of the dominant pulsation mode in a frequency spectrum of the extracted light curve as a metric, S/N_{f_1} . This relies on calculating periodograms for each pixel, in a similar manner to the public `TESS_LOCALIZE` software package (Higgins & Bell 2023). In essence, larger aperture masks maximise the extracted flux of a target, hence generally also maximise the signal in the resultant S/N of pulsation mode amplitudes. Yet, over-large target aperture masks increase the noise contribution, which could decrease the overall S/N of pulsation modes, especially for fainter stars. Moreover, this pulsation-optimised mask selection is important for variable stars, such as SPB stars, because they can be high-amplitude multi-periodic pulsators with long-period beating patterns (see e.g. Pápics et al. 2015, 2017), and appreciably affect the size of the optimal aperture mask from cadence to cadence.

The optimised target aperture mask was decided by testing the S/N of the dominant pulsation mode in the frequency spectra of light curves extracted using different aperture sizes. The S/N is defined as the height of the highest-amplitude peak divided by the mean amplitude within the frequency spectrum ranging from 0 to 6 d^{-1} . This frequency range was chosen since prograde dipole modes of SPB stars are typically observed between about 1 and 3 d^{-1} (Szewczuk et al. 2021; Pedersen et al. 2021). Non-linear combination frequencies and harmonics typically occur at higher frequencies, and appear as groups as discussed by Kurtz et al. (2015). The larger sample of *Kepler* SPB stars studied by Pedersen et al. (2021) also supports this range for the noise window, since the period spacing patterns extracted for such stars are consistently found to have periods ranging from 0.3 to 3 d (i.e. $0.33 < \nu < 3.3 \text{ d}^{-1}$).

We begin by first extracting the light curve from only the central pixel containing the target star. The S/N of the dominant pulsation frequency in the resultant periodogram is thus used as a benchmark value to compare against, such that aperture masks with improved S/N are favoured. Next we successively test the change in the resultant S/N of the dominant pulsation frequency in the periodogram for larger aperture masks by adding rings of pixels, as shown in Fig. 2.

² <https://archive.stsci.edu/missions-and-data/tess>

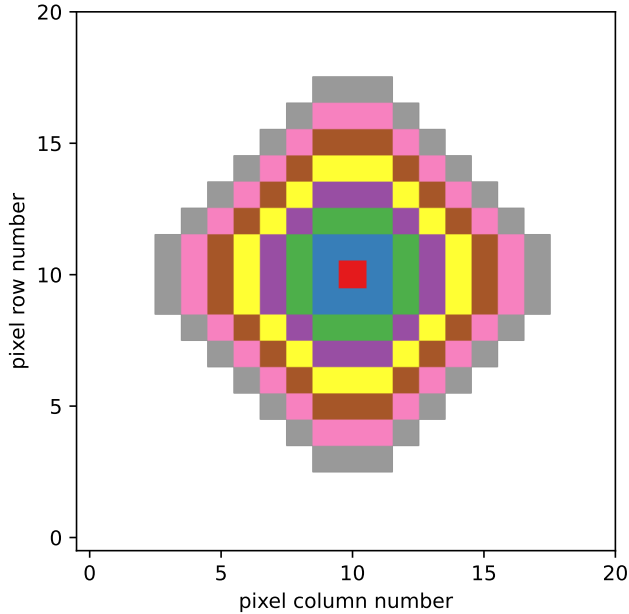


Figure 2. Pixel rings used for iteratively determining each target’s optimal aperture size, which are represented in different colours. In this schematic, the target star is located at pixel (10,10), shown as the central red pixel.

The aperture with the highest S/N_{f_1} was chosen as the optimal aperture. For each target aperture defined, we define the background to exclude any pixels within the target aperture. Finally, to detrend our light curves of any systematic trends, we test the optimal number of principal components (PCs) to remove, also in an iterative fashion, again maximising S/N_{f_1} based on the optimal target aperture mask — see Sec. 2.2.2 for details of this process. As our method optimises the target’s aperture mask and approach to detrending based on the S/N of a star’s pulsation frequencies, it is better suited to the problem of asteroseismology of early-type stars, as opposed to only using a flux-based threshold to define a target aperture mask that does not account for variability.

2.2.2 Light curve detrending

To study stellar pulsations in a light curve, they first need to be disentangled from variability caused by instrumental effects. These include the heating or cooling of the detector after and before the telescope reorients itself with respect to the Sun, as well as time-dependent scattered light. These trends can be removed, somewhat subjectively, using methods such as fitting a spline or a low-order polynomial leaving only the astrophysical variability behind (e.g. Pápics et al. 2017; Bowman et al. 2018). Alternative methods for detrending light curves include Gaussian process regression (see e.g. Aigrain et al. 2016) and the increasingly popular approach of principal component analysis (PCA; Lightkurve Collaboration et al. 2018).

We have chosen to detrend our light curves using an PCA approach as this has proven powerful for TESS light curves of early-type pulsating stars (see e.g. Bowman et al. 2022; Burssens et al. 2023). In our case, the PCs are light curve shapes that when multiplied by a coefficient and summed can reconstruct the background light curve. This model for the background flux can be written as

Table 2. The TESS sectors used in defining chunks of light curves

KIC ID	TESS sectors used		
	chunk 1	chunk 2	chunk 3
3240411	81, 82	74	54, 55
3459297	81, 82	74, 75	54, 55
4930889	81, 82	74, 75	54, 55
5941844	80, 81	53, 54	40, 41
6352430	80, 81, 82	74, 75	53, 54, 55
7760680	81, 82	74, 75	54, 55
8766405	81, 82	74, 75	54, 55
11360704	81, 82, 83	74, 75, 76	54, 55, 56

$$F_{\text{bg}}(t) = \sum_n a_n C_n(t), \quad (1)$$

where $F_{\text{bg}}(t)$ is the approximated background light curve flux, $C_n(t)$ are the PCs, a_n are their coefficients, and n is the number of PCs used (see Lightkurve Collaboration et al. 2018). Each successive PC contains a smaller fraction of the variance in a light curve, and we find that $n \leq 8$ is consistently sufficient for SPB stars observed in TESS mission data. We calculated the PCs of background pixels using the LIGHTKURVE software tool (Lightkurve Collaboration et al. 2018), then removed them from the target star’s light curve. We emphasize that this detrending was performed before any analysis of a periodogram — i.e. before calculating the S/N of pulsation frequencies in the aperture optimisation step (c.f. Section 2.2.1) or for before making S/N maps (e.g. Fig. 3).

For individual pixels and testing different aperture sizes, the first three PCs of the background were used as a starting point when detrending. We decided that three PCs was sufficient based on inspection of pixel light curves and the typical structure of the PCs. In this first pass, the background pixels were defined as those with below-median flux (c.f. Section 2.2.1). Then, pixels with $S/N_{f_1} > 3$ were excluded from the background and the light curve of the target star was extracted. The number of PCs used in detrending the target light curve was then optimised in an iterative fashion to maximise S/N_{f_1} .

As a demonstration, we show a summary figure of the application of this multi-step curve-of-growth process to extracting light curves applied to KIC 7760680 in Fig. 3, in which the lower-left panel shows the value of S/N_{f_1} as the number of pixel rings is increased during the mask optimisation step. The middle two panels of Fig. 3 show the PCs and the light curves detrended with the corresponding number of PCs. The lower-right panel shows how S/N_{f_1} varies with the number of PCs, with a maximum at three PCs, hence defining the optimal number for TESS sector 82 of KIC 7760680. This results in $S/N_{f_1} = 34.43$ for the optimised light curve, versus $S/N_{f_1} = 33.91$ for the TESS quick-look pipeline (QLP) light curve. Using our extraction method, the S/N of the dominant mode is on average 4 per cent higher than using NASA’s SPOC-pipeline light curve and 18 per cent higher than the QLP light curve, which are also available on the MAST archive, across our sample of SPB stars.

2.2.3 Joining TESS sectors

Each of the eight SPB stars in our sample was observed by TESS from one to three consecutive sectors, which we refer to as chunks, with then a large gap of 2 yr before TESS re-observes the same star once again. We have concatenated the detrended light curves from

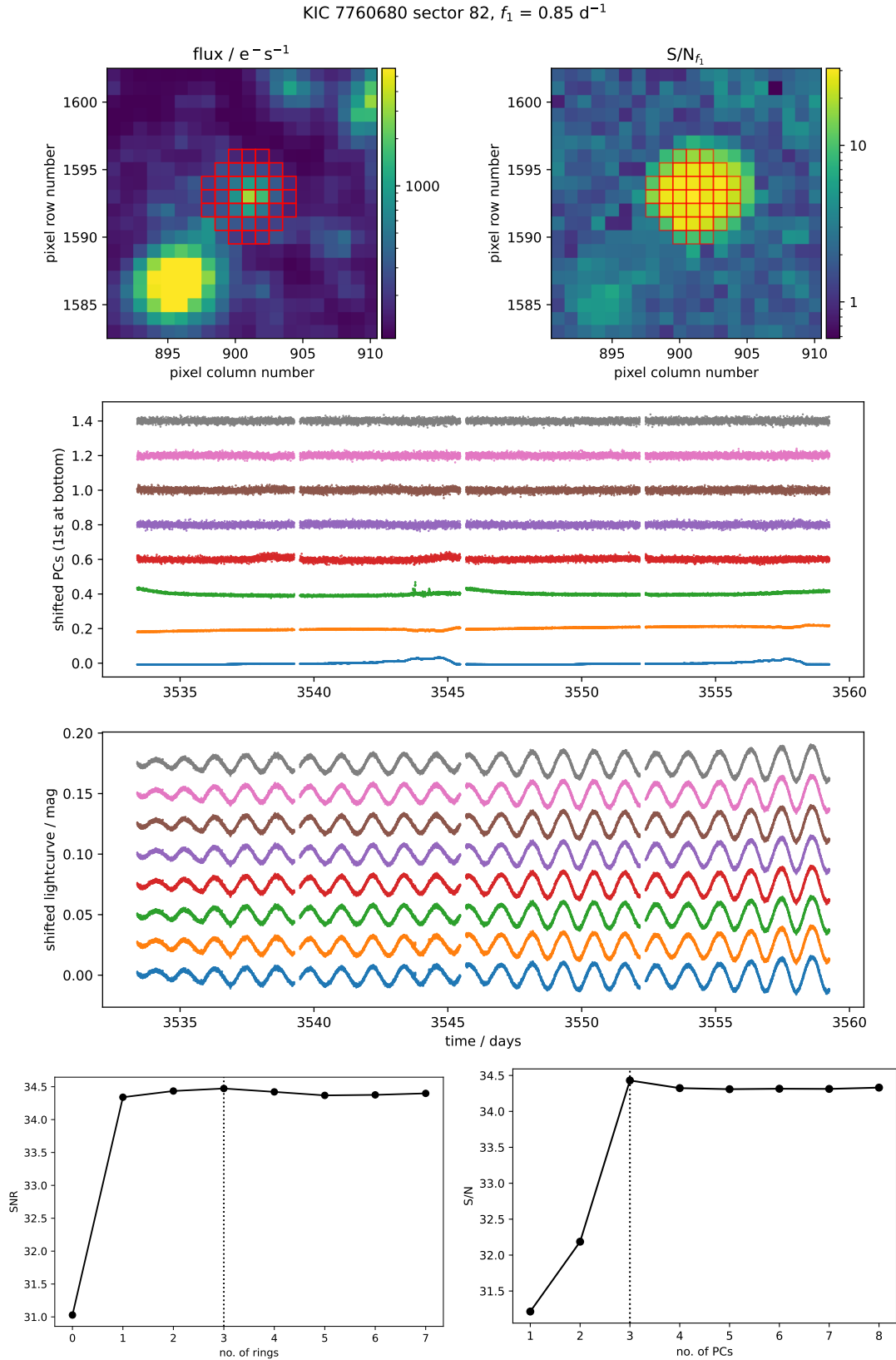


Figure 3. TESS light curve extraction summary of sector 82 for KIC 7760680. The target aperture mask that maximises the S/N of the dominant pulsation mode is highlighted in red in the top two panels, with left- and right-hand panels showing flux and S/N, respectively. The second and third rows show the principal components (PCs) and corresponding detrended light curves, noting that the first PC is shown at the bottom of the panel. The bottom-left and -right panels show the curve-of-growth for the number of concentric rings in determining the optimal pixel mask and the number of PCs, respectively.

individual sectors into longer light curves spanning one, two and three chunks of data. The sectors included in each chunk sometimes differ across our sample because of where a star falls precisely in TESS’s field of view, and are listed in Table 2. We note that some stars are observed in some sectors that were discarded because the target was too close to the edge of the detector, thus yielding unusable data. In the case of KIC 5941844, this meant that there was a particularly long gap between chunk 1 and chunk 2.

Due to the improvement in the TESS FFI cadence after the end of cycle 2 (i.e. after sector 55) from 10 min to 200 sec, we binned all data to have a 10-min cadence for consistency purposes. This was done before concatenation of different chunks by taking the mean flux in each 10-min bin. This is important because a different (average) cadence defines a different Nyquist frequency and amplitude suppression function (Bowman 2017), as well as to avoid having to assign different weights to data points in subsequent Fourier analysis because of the different integration times.

2.3 Frequency extraction from optimal light curves

To investigate how the length of a TESS light curve impacts frequency analysis, we made three light curves for each star: the first using only chunk one, the next using chunks one and two, and the last using all three chunks, as detailed in Table 2. Each of these light curves was transformed into frequency space by means of a discrete Fourier transform, using the PERIOD04 software package (Lenz & Breger 2005). We extracted significant pulsation frequencies following the standard approach of iterative pre-whitening in order of decreasing amplitude until the significance criterion of S/N of 4.6 in amplitude was reached and performed a non-linear multi-sinusoid least-squares optimisation (see e.g. Kurtz et al. 2015; Bowman & Michielsen 2021). For frequency extraction, we defined S/N as the amplitude height of a peak in the frequency spectrum divided by the mean amplitude within a 2 d^{-1} frequency window centred on the peak. The noise window is therefore smaller compared to the calculation of S/N_{f_1} , which encompassed the entire frequency range up to 6 d^{-1} in order to test the effectiveness of detrending. The frequency extraction process was performed for each of the one-, two- and three-chunk light curves for each star. We provide a list of extracted significant frequencies and mark those that are consistent across the TESS and *Kepler* light curve analyses in Tables A1–A8 in Appendix A.

As a first result on the efficacy of using TESS for g-mode asteroseismology, we compared our extracted g-mode frequencies using TESS light curves to those identified by Pedersen et al. (2021) in *Kepler* mission data. Additionally, we tested if our extracted frequencies belong to the period spacing pattern identified by Pedersen et al. (2021) using *Kepler* light curves. We determine the fraction of frequencies we recover in TESS light curves compared to the period spacing pattern reported by Pedersen et al. (2021) based on *Kepler* data for each star, which is detailed in Table 3. In this way, we quantify the agreement between detectable significant pulsation frequencies for short TESS light curves compared to long *Kepler* light curves. Our results of how the number of recovered pulsation frequencies in a star’s period spacing pattern depends on the amount of TESS data is shown graphically in Fig. 4. Overall, we find that each SPB star requires a different amount of TESS data to satisfactorily reproduce the period spacing pattern extracted using *Kepler* data, if at all. For example, two sectors (i.e. only one chunk) of TESS data for KIC 4930889 yields a 25 per cent agreement, which rises rapidly to over 60 per cent agreement for six sectors (i.e. three chunks) of TESS data. On the other hand, additional chunks for KIC 8766405 does not improve the recovery rate of 10 per cent. Whilst it is generally

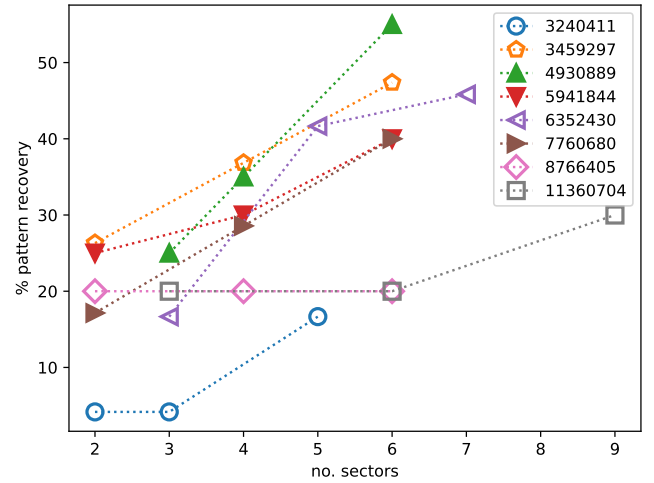


Figure 4. Percentage of frequencies in the *Kepler* period spacing patterns reported by Pedersen et al. (2021) that were extracted in our analysis of TESS light curves. We were able to find period spacing patterns for the stars with filled symbols. The length and quality of the data was insufficient to find a convincing pattern in the TESS light curves for stars with open symbols.

the case that more TESS sectors are better for frequency analysis of early-type stars, our results demonstrate that it strongly depends on the duty cycle of the combined light curve and the pulsation frequencies of a star on whether additional sectors allow one to converge (or diverge) from the true period spacing pattern. We discuss all stars individually in Section 3.

Up until now, we have been guided in our frequency recovery analysis by heavily relying on the reported period spacing patterns from Pedersen et al. (2021) based on 4 yr of *Kepler* data. To evaluate potential biases, we next performed an independent analysis to construct period spacing patterns based solely on the TESS light curves, avoiding any knowledge or biases of what the period spacing pattern ‘should’ look like. We do this because the choice of which frequencies to include in the pattern is subjective, and the inclusion of ambiguous frequencies may propagate errors into the final modelling results, as discussed by Michielsen et al. (2021) and Bowman & Michielsen (2021).

2.3.1 Period spacing pattern fitting

It is well established that faster rotation in the near-core region where g modes are most sensitive, f_{rot} , produces a stronger negative gradient in a period spacing pattern of prograde dipole (i.e. $\{\ell, m\} = \{1, 1\}$) g modes in the observer’s inertial reference frame (Aerts 2021). This means that the period spacing patterns are generally more difficult to extract for faster rotating stars (see Pápics et al. 2017; Szweczk et al. 2021) and benefit from longer light curves.

The asymptotic period spacing value, Π_0 , is related to a star’s mass and age, and is defined as

$$\Pi_0 = 2\pi^2 \left(\int_{r_1}^{r_2} \frac{N(r)}{r} dr \right)^{-1}, \quad (2)$$

where r is the radius of a star, r_1 and r_2 are the radial positions of the g-mode cavity, and $N(r)$ is the Brunt-Väisälä frequency (Aerts 2021). The parameter Π_0 has also been called the buoyancy travel time, and it directly probes the thermal and chemical composition structure in the near-core region through its dependence on $N(r)$. Through a

Table 3. Number of pulsation frequencies extracted for each star and the number of frequencies which are part of the period spacing pattern reported by Pedersen et al. (2021). Quantities are shown for each number of chunks in the light curve.

KIC ID	Number of extracted frequencies			Number of extracted frequencies in pattern		
	1 chunk	2 chunks	3 chunks	1 chunk	2 chunks	3 chunks
3240411	1	6	12	1	1	4
3459297	8	9	12	5	7	9
4930889	8	14	25	5	7	11
5941844	8	13	16	5	6	8
6352430	13	23	28	4	10	11
7760680	10	15	18	6	10	14
8766405	15	20	14	2	2	2
11360704	16	24	14	2	2	3

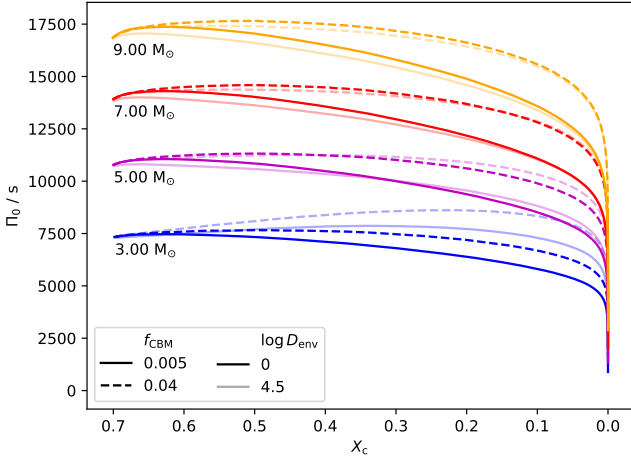


Figure 5. The evolution of the asymptotic period spacing, Π_0 , with central hydrogen mass fraction, X_c , for selected masses within the grid of structure models used in this work. The value of CBM, f_{CBM} , is indicated by either solid or dashed lines. The amount of the envelope mixing, D_{env} , is indicated by either saturated or pale colour.

comparison to grids of theoretical models, and the dependence of Π_0 on $N(r)$, the mass, core mass, and age of a star can be determined. We show values from representative models in our grid of structure models in Fig. 5. We used the open-source AMIGO³ software tool (Van Reeth et al. 2016, 2018, 2022) to fit the extracted period spacing patterns of the SPB stars in our sample, and determine the near-core rotation frequency, f_{rot} , and the asymptotic period spacing, Π_0 . We report the values of Π_0 and f_{rot} in Table 4.

2.4 Forward asteroseismic modelling

To perform forward asteroseismic modelling, we make use of the grid of structure models calculated by Johnston et al. (2019), who used Π_0 as a seismic diagnostic in their study of three eclipsing binaries containing g-mode pulsators. The grid contains 770 000 structure models calculated using the open-source MESA⁴ stellar structure and evolution software package (Paxton et al. 2011, 2013, 2015, 2018). The grid spans a mass range of 1.2 to 9 M_{\odot} , with an interval of 0.1 M_{\odot} below a mass of 5 M_{\odot} and 0.25 M_{\odot} above. The models were

calculated with a metallicity of $Z = 0.014$ and a mixing length theory (MLT) parameter of $\alpha_{\text{MLT}} = 1.8$, which is expressed in terms of pressure scale heights. The varied parameters were mass, CBM parameter f_{CBM} , and envelope mixing parameter D_{env} (Johnston et al. 2019). The CBM parameter takes the form of an exponentially decaying diffusion coefficient (Freytag et al. 1996), with f_{CBM} determining the gradient of the efficiency in the near-core mixing region. The envelope mixing is based on a diffusion coefficient that emulates gravity wave mixing with $D(r) \propto \rho^{-1}$ (see Rogers & McElwaine 2017), such that the values of D_{env} is the diffusion coefficient at the interface of the CBM region and the envelope. f_{CBM} ranges between 0.005 to 0.040 in intervals of 0.005 and $\log(D_{\text{ext}}/\text{cm}^2 \text{ s}^{-1})$ ranges between 0.0 and 4.5 in intervals of 0.5. The models each had 600 time steps, beginning in the pre-main sequence and finishing at the end of the main sequence. The pre-main sequence phase lasted for approximately 250 time steps, but we exclude this in our forward asteroseismic modelling given that Pedersen et al. (2021) concluded that our SPB stars are core-hydrogen burning.

For those stars for which we identified a period spacing pattern (listed in Table 4), we fit our Π_0 values to a grid of models calculated by Johnston et al. (2019) developed for g-mode forward asteroseismic modelling. The fit was performed in combination with literature values of effective temperature, T_{eff} , and surface gravity, $\log g$, as additional observables (Pápics et al. 2013, 2015; Hanes et al. 2019; Gebruers et al. 2021).

We used the Mahalanobis distance (MD) as a merit function,

$$\text{MD} = (Y_{\text{mod}} - Y_{\text{obs}})^{\top} (V + \Lambda)^{-1} (Y_{\text{mod}} - Y_{\text{obs}}), \quad (3)$$

where Y_{mod} and Y_{obs} are vectors containing the model and observed values of Π_0 , T_{eff} and $\log g$, respectively, V is the variance-covariance matrix for the fitted quantities calculated from the model grid, and Λ is the square matrix containing the squared errors on the fitted quantities in its diagonals (Aerts et al. 2018). We use MD as a merit function instead of χ^2 in this case since it has the significant advantage of incorporating correlations and degeneracies amongst parameters (Aerts et al. 2018). The MD hence disfavours models with atypical combinations of fitted values, unlike χ^2 which treats all parameters as uncorrelated and independent. Michielsen et al. (2021) demonstrate the limitations of using χ^2 and benefits of using MD as merit function in forward asteroseismic modelling of g modes in SPB stars.

We use Bayes' theorem to calculate the probability distribution of models given our observed values, for which we use the likelihood

$$\mathcal{L}(Y_{\text{obs}}|\theta) \propto \exp(-0.5(\det(V + \Lambda) + 2k\pi + \text{MD})), \quad (4)$$

where $k = 3$ is the number of fitted parameters, and θ is the set of grid parameters (i.e. mass, f_{CBM} , D_{env} and central hydrogen fraction,

³ <https://github.com/TVanReeth/amigo>

⁴ <https://docs.mesastar.org/en/latest/>

X_c). We assume the unnormalised prior probability, $P(\theta)$, is flat in all dimensions. Using Bayes' theorem, the probability of a set of grid parameters θ given the observations Y_{obs} is then

$$P(\theta|Y_{\text{obs}}) = \frac{P(\theta)\mathcal{L}(Y_{\text{obs}}|\theta)}{\sum_i P(\theta)\mathcal{L}(Y_{\text{obs}}|\theta)}. \quad (5)$$

The $1\text{-}\sigma$ confidence intervals for each parameter of the best model can be found using the minimum and maximum values of θ for those models with $P(\theta|Y_{\text{obs}})$ above the 68th percentile. Similarly to Johnston et al. (2019), confidence intervals for the best-fitting mass, age, and core mass of SPB stars based on MD and using Π_0 in this manner are quite large, and incorporate a sizeable fraction of the MESA grid. However, since the MD is a maximum likelihood estimation (MLE) method, the best-fitting values are useful and informative to compare between TESS and *Kepler* modelling results.

3 RESULTS

Our analysis of the TESS light curves of the eight SPB stars yielded between 1 and 28 extracted frequencies depending on the star, as shown in Table 3. This demonstrates that success in the application of iterative pre-whitening to extract coherent pulsation mode frequencies in intermittent TESS light curves is very star dependent. We provide details on the specifics of the extracted frequencies for each star in App. A, and the frequencies are plotted on pre-whitened spectra in App. B. Due to the reduction in noise, more frequencies were extracted for light curves with more chunks. However, the gaps between chunks introduced complexity in the spectral window, making the iterative pre-whitening more difficult.

We examined our extracted frequencies for matches with those in the period spacing patterns of Pedersen et al. (2021). This is shown in the final three columns of Table 3. We judged matches based on similarity in both frequency and relative amplitude compared to other modes. The number of matches with the Pedersen et al. (2021) patterns generally increased with the number of chunks. The percentage of recovery as a function of the number of chunks for each star is shown in Fig. 4.

Our Π_0 values and core rotation rates from fitting the period spacing pattern using AMIGO are shown in Table 4, along with the spectroscopic constraints used in our fitting. For the two-chunk data of KIC 7760680, our core rotation rate of $0.48 \pm 0.02 \text{ d}^{-1}$ is remarkably similar to the value of $0.455 \pm 0.022 \text{ d}^{-1}$ reported by Pedersen et al. (2021) and $0.4790^{+0.0066}_{-0.0094} \text{ d}^{-1}$ reported by Moravveji et al. (2016), both using the 4-yr *Kepler* light curves. The rotation rates of other stars, whilst being relatively high precision constraints, do not agree within 1σ between our work and the values reported by Pedersen et al. (2021). This demonstrates how it is possible to achieve high precision but low accuracy in measuring near-core rotation rates from period spacing patterns, because of the potential subjectivity and data quality issues when manually building period spacing patterns.

The results of forward asteroseismic modelling based on the MD as merit function and a comparison of observed and theoretically predicted Π_0 , T_{eff} and $\log g$ parameters for all stars are shown in Tables 6 and 7. In these tables, we provide the best-fitting mass, convective core mass, and central hydrogen fraction, along with the 68th percentile confidence intervals (i.e. 1σ) calculated using Eq. 5. The values of f_{CBM} and D_{ext} were largely unconstrained in all cases, similar to Johnston et al. (2019), so are not included in Table 6. The results for individual stars are discussed in Section 3.2.

For KIC 4930889, KIC 5941844, and KIC 7760680, we were able

to find period spacing patterns using the TESS mission light curves. Our modelling results are compatible to those reported by Pedersen et al. (2021) based on 4-yr *Kepler* light curves. The results of forward asteroseismic modelling are provided in Table 6, and the stars are discussed individually in Section 3.2. However, we did not extract a robust period spacing pattern using a 'blind search' approach for the other five SPB stars in our sample, due to a combination of complex spectral windows and higher noise than the *Kepler* light curves. For KIC 3459297 and KIC 6352430 we were able to use the frequencies from the Pedersen et al. (2021) patterns to inform our extraction of frequencies in the TESS light curves and successfully determine a compatible Π_0 value. The results of the fits for these 'informed' stars are shown in Table 7. Summary figures of the forward asteroseismic modelling for all stars with successful period spacing pattern extraction are provided in Appendix B. We discuss the modelling results for KIC 3459297 and KIC 6352430 in Section 3.3. For KIC 3240411, KIC 8766405 and KIC 11360704, we only recovered two to three frequencies (see Table 3 and Fig. 4), so we were unable to continue our analysis using the TESS data, and thus do not report any forward asteroseismic modelling results.

3.1 Reanalysis of Kepler data

In their approach to forward asteroseismic modelling, Pedersen et al. (2021) using the MD to fit individual observed frequencies to theoretical counterparts calculated by models. Whereas in this work, owing to the frequency resolution issues of TESS mission light curves, we opt to model the stars using the global asteroseismic parameter, Π_0 . Therefore, to compare like to like, we reanalysed the *Kepler* light curves using our light curve extraction method, the only difference being the background detrending. Since the *Kepler* target pixel file data usually contain far fewer pixels than the 20 by 20 TESS full-frame image cutouts, we often did not have enough background pixels to perform PCA effectively. Thus we instead detrended the background systematics using a smoothed cubic spline fit. We performed frequency extraction of the *Kepler* light curves using iterative pre-whitening in the same way as we did for the TESS data, and determined values of Π_0 from the same period spacing patterns reported by Pedersen et al. (2021) of 5427 ± 1102 , 10763 ± 730 and $8843 \pm 1180 \text{ s}$ for KIC 4930889, KIC 5941844 and KIC 7760680, respectively. The best-fitting parameters for these stars are listed in Table 5. Our *Kepler* light curve analysis and forward asteroseismic modelling results based on Π_0 are consistent with the parameters reported by Pedersen et al. (2021) based on individual frequency fitting. The only difference is that we find a somewhat lower value of X_c for KIC 4930889, but as expected, the confidence intervals based on fitting Π_0 are quite large.

3.2 Stars with clear period spacing patterns

Using a completely 'blind' approach, we successfully extracted period spacing patterns for KIC 4930889, KIC 5941844 and KIC 7760680 using TESS mission light curves that yield compatible Π_0 , masses, ages and core masses to those reported by Pedersen et al. (2021) based on 4-yr *Kepler* light curves. These stars, being in our good sample, are all bright with high amplitude pulsations. For KIC 7760680, we found patterns in the two and three chunk data, whereas for KIC 4930889 and KIC 5941844, we only identified a pattern in the three chunk data.

When performing forward asteroseismic modelling of KIC 4930889, we discovered that the confidence intervals encompassed the whole range for mass and central hydrogen fraction,

Table 4. Values for f_{rot} and Π_0 obtained from fitting the period spacing pattern, as well as the literature spectroscopic constraints that were used in the forward asteroseismic modelling. In general, Π_0 values are derived from the three-chunk light curves in this work, apart from the starred row that used the two chunk light curve for comparison purposes. The final column provides the literature reference for T_{eff} and $\log g$. The period spacing patterns for the last two stars were informed by those of Pedersen et al. (2021), because identifying a reliable period spacing pattern from the TESS data alone was not feasible.

KIC ID	$f_{\text{rot}} / \text{d}^{-1}$	Π_0 / s	$T_{\text{eff}} / \text{K}$	$\log(g / \text{cm s}^{-2})$	reference
4930889	0.35 ± 0.17	2944 ± 893	15100 ± 150	3.95 ± 0.1	Gebruers et al. (2021)
5941844	0.47 ± 0.01	17612 ± 18	14025 ± 300	4.24 ± 0.08	Gebruers et al. (2021)
*7760680	0.48 ± 0.02	9281 ± 1281	11650 ± 210	3.97 ± 0.08	Pápics et al. (2015)
7760680	0.54 ± 0.02	12194 ± 306	11650 ± 210	3.97 ± 0.08	Pápics et al. (2015)
3459297	$0.00^{+1.04}$	2132 ± 1985	13100 ± 600	3.61 ± 0.14	Hanes et al. (2019)
6352430	0.53 ± 0.11	8390 ± 3839	12810 ± 200	4.05 ± 0.05	Pápics et al. (2013)

Table 5. Comparison of modelling results fitting Π_0 from Kepler data to the Pedersen et al. (2021) results.

KIC ID	model fits – Kepler (Pedersen et al. 2021)			model fits – Kepler (this work)		
	M/M_{\odot}	M_c/M_{\odot}	X_c/X_{ini}	M/M_{\odot}	M_c/M_{\odot}	X_c/X_{ini}
4930889	4.135 ± 0.493	0.62	0.39 ± 0.10	$4.4^{+4.6}_{-3.2}$	$0.87^{+1.41}_{-0.87}$	$0.58^{+0.41}_{-0.58}$
5941844	3.559 ± 0.089	0.85	0.89 ± 0.06	$3.6^{+3.4}_{-2.4}$	$0.78^{+1.18}_{-0.78}$	$0.87^{+0.12}_{-0.87}$
7760680	3.466 ± 0.081	0.62	0.64 ± 0.17	$3.2^{+2.8}_{-2.0}$	$0.44^{+0.88}_{-0.44}$	$0.44^{+0.55}_{-0.44}$

Table 6. Comparison of modelling results for stars with period spacing patterns found in a blind search of frequencies extracted from TESS data. Results marked with ‘*’ used the Π_0 value from the two chunk light curve, whereas all others used the three chunk light curve.

KIC ID	model fits – Kepler (Pedersen et al. 2021)			model fits – TESS (this work)		
	M/M_{\odot}	M_c/M_{\odot}	X_c/X_{ini}	M/M_{\odot}	M_c/M_{\odot}	X_c/X_{ini}
4930889	4.135 ± 0.493	0.62	0.39 ± 0.10	$4.4^{+4.6}_{-3.2}$	$0.87^{+1.41}_{-0.87}$	$0.57^{+0.41}_{-0.57}$
5941844	3.559 ± 0.089	0.85	0.89 ± 0.06	$3.6^{+3.4}_{-2.4}$	$0.78^{+1.18}_{-0.78}$	$0.87^{+0.12}_{-0.87}$
7760680	3.466 ± 0.081	0.62	0.64 ± 0.17	$*3.2^{+2.8}_{-2.0}$	$*0.44^{+0.88}_{-0.44}$	$*0.44^{+0.55}_{-0.44}$
				$3.2^{+2.8}_{-2.0}$	$0.44^{+0.88}_{-0.44}$	$0.44^{+0.55}_{-0.44}$

X_c , as shown in Table 6. The core mass was better constrained, with the upper limit of the 1σ confidence interval at $2.29 M_{\odot}$; the highest core mass in our grid is $2.75 M_{\odot}$. Despite our larger uncertainties, our best-fitting model has parameters that are within 1σ of those reported by Pedersen et al. (2021) for the mass, and within 2σ for central hydrogen fraction. It is known that generally large confidence intervals based on forward asteroseismic modelling using Π_0 and the MD as merit function (Johnston et al. 2019), so this is not unexpected. This is because Π_0 is sensitive to many other parameters (e.g. mass, age and mixing), thus degenerate within the HR diagram.

For KIC 5941844, we found a very high value of $\Pi_0 = 17612 \pm 18$ s, which is at the upper end of the possible values in our grid (see Fig. 5). Such a high value of Π_0 is unlikely for a low-mass SPB star (e.g. Bowman 2020). Nonetheless, we recovered best-fitting model parameters from forward asteroseismic modeling that are remarkably similar to those reported by Pedersen et al. (2021), as shown in Table 6.

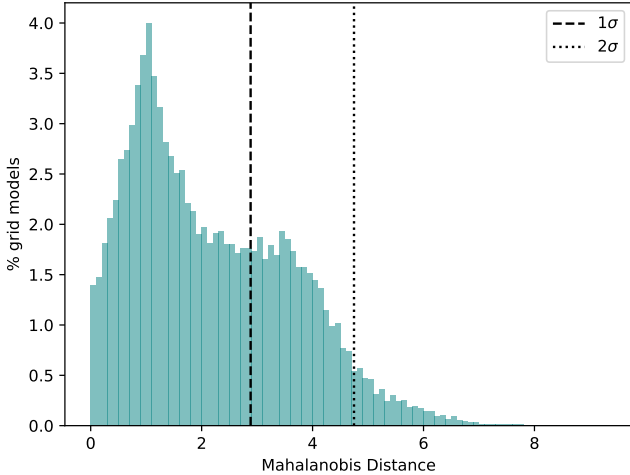
The final good SPB star in our sample is KIC 7760680, which is the most well studied SPB star in the Kepler mission data set. It currently holds the record for the longest period spacing pattern of

36 consecutive radial order g modes in an SPB star (Moravejji et al. 2016; Michielsen et al. 2021; Bowman & Michielsen 2021; Pedersen et al. 2021). For KIC 7760680, we successfully measured Π_0 values of 9281 ± 1281 s and 12194 ± 306 s from the two- and three-chunk data sets, respectively. Our forward asteroseismic modelling yielded a best fit mass that is within 3σ of the Pedersen et al. (2021) results, and within 2σ for X_c . Using the two-chunk light curve (marked with a ‘*’ in Table 6) we find the same best model as the modelling based on the three chunk light curve. The scatter in modelling results for both this analysis and various other literature can be seen in the bottom panel of Fig. B6.

We find large uncertainty limits on our best fit model parameters, similar to Johnston et al. (2019) who also fit Π_0 rather than individual frequencies. This is due to the marginalisation of the probability distribution over individual parameters, which effectively assigns the entire error budget to that parameter. More detailed information on the constraining power of our fit can be seen in the distribution of MD values, which is shown for the two chunk light curve of KIC 7760680 in Fig. 6. The number of models with the lowest MD values is small, at around 1.5 per cent of the grid, meaning that the best model is still well-constrained. Hence, we are able to successfully recover best fit

Table 7. Same as Table 6, but for stars with period spacing patterns informed by the patterns reported by Pedersen et al. (2021).

KIC ID	model fits – <i>Kepler</i> (Pedersen et al. 2021)			model fits – TESS (this work)		
	M/M_{\odot}	M_c/M_{\odot}	X_c/X_{ini}	M/M_{\odot}	M_c/M_{\odot}	X_c/X_{ini}
3459297	3.876 ± 0.690	0.25	0.24 ± 0.13	$4.4^{+4.1}_{-3.2}$	$0.61^{+1.00}_{-0.61}$	$0.24^{+0.44}_{-0.24}$
6352430	3.333 ± 0.171	0.40	0.36 ± 0.21	$3.4^{+3.4}_{-2.2}$	$0.62^{+1.01}_{-0.62}$	$0.63^{+0.36}_{-0.63}$

**Figure 6.** Percentage of grid models at different Mahalanobis distances when fitting Π_0 from the two chunk light curve of KIC 7760680.

models consistent with the results of Pedersen et al. (2021) despite our larger uncertainty limits.

3.3 Stars with period spacings informed by those reported by Pedersen et al. (2021)

We did not initially identify a period spacing pattern in the extracted frequencies for KIC 3459297 and KIC 6352430. For KIC 3459297, we were able to match nine of the frequencies from the three chunk data to the period spacing pattern reported by Pedersen et al. (2021) to determine Π_0 . However, due to gaps in the pattern and a very few consecutive radial orders identified, and we were only able to use four period spacings in the fit. This naturally produces a large relative error for Π_0 when fitting the period spacing pattern with AMIGO. Our best-fitting model for this star from forward asteroseismic modelling is within 1σ of the Pedersen et al. (2021) best model, but the confidence intervals on the parameters are large, as shown in Table 7.

For KIC 6352430, we also could not find a reliable period spacing pattern with a ‘blind’ approach, but were able to match some frequencies in the TESS light curve to members of the period spacing pattern reported by Pedersen et al. (2021) using 4-yr *Kepler* data. The recovery fraction of pulsation frequencies in the pattern was relatively high, at nearly 50 per cent (see Fig. 4). However, we did not recover the important lower-amplitude frequencies which are needed to accurately constrain Π_0 . We fitted four period spacings, mostly in the lower period range, and found $\Pi_0 = 8390 \pm 3839$ s. Our best-fitting model for this star from forward asteroseismic modelling is within 1σ of the Pedersen et al. (2021) best model, but the confidence intervals on the parameters are large, as shown in Table 7.

4 DISCUSSION AND CONCLUSIONS

In this work, we have developed and applied a new method to extract TESS light curves of pulsating early-type stars. Our method used the S/N of the dominant pulsation mode to determine the optimum aperture, and often resulted in a different aperture than would be obtained using the commonly employed flux threshold approach (see top panels of Fig. 3). By optimising aperture mask based on the S/N of pulsations in the resultant frequency spectrum in this way, we maximise the ability to extract as many frequencies as possible from the final light curves. This is important for subsequent frequency analysis, as well as determining accurate values of Π_0 and performing forward asteroseismic modelling. Indeed, asteroseismic observables such as Π_0 are most constraining when derived from uninterrupted g-mode period spacing patterns spanning a large number of consecutive radial orders.

We extracted frequencies from TESS light curves with different lengths (i.e. 1, 2 and 3 chunks of consecutive TESS sectors) for a sample of eight SPB stars originally studied using *Kepler* mission data, and compared the TESS frequencies to those in the period spacing patterns reported by Pedersen et al. (2021). We found between 5 and 55 per cent of the *Kepler* pulsation frequencies within the period spacing patterns were recovered in our TESS light curve extraction. The brightest stars with the highest-amplitude pulsations performed better in the frequency recovery fraction, although adding more chunks of data did not always improve this. In some cases, adding more sectors did not increase the percentage of completeness of the pattern. This demonstrates that whilst it is commonly quoted as ‘the more data the better’ in asteroseismology, it is highly star-dependent on how many TESS sectors are needed to accurately extract a g-mode period spacing pattern. For example, we recovered period spacing patterns in three stars, despite recovering less than 60% of the pattern for KIC 4930889 and less than 40% of the pattern for KIC 5941844 and KIC 7760680. We find that the overall success of TESS data in providing modelling results similar to *Kepler* is highly dependant on the individual star. The trade-off between lower noise and higher complexity is apparent for KIC 7760680, for which we extracted period spacing patterns for both the two and three chunk data and demonstrate only a marginal improvement in pattern recovery, with the same modelling results.

We determined Π_0 values from the period spacing patterns for our TESS data, and combined these with spectroscopic constraints from the literature to perform forward asteroseismic modelling. Our best-fitting model results are largely consistent with the parameters reported by Pedersen et al. (2021), although our confidence intervals were much larger and generally capture a sizeable fraction of the theoretical grid of models. This was expected (see Johnston et al. 2019) given the degeneracy of Π_0 across the parameter space (i.e. mass and age) in the HR diagram. Moreover, this underpins the power but potential drawbacks of individual frequency fitting in forward asteroseismic modelling. For example, our use of Π_0 as an observable has some advantages over individual frequency fitting, such that it probes the bulk density profile over the near-core region making it

is less susceptible to sharp local minima in the posterior parameter space compared to individual frequency fitting. On the other hand, such sharp features provide finer detail on the interior physics of stars. In this sense, fitting with Π_0 could be described as low-precision high accuracy and potentially vice versa for individual frequency fitting — see discussion by Bowman & Michielsen (2021).

Our results demonstrate the potential biases in the methods of asteroseismology that intermittent TESS data alone can be prone to. For example, those stars for which we found period spacing patterns in TESS data were all bright with no nearby contaminating neighbours. However, KIC 8766405 was also in our ‘good’ sample, but we were not able to find a period spacing pattern due to the intermittent TESS data not having sensitivity to the presence of low-amplitude modes in the period spacing pattern reported by Pedersen et al. (2021). Selecting bright, isolated stars is a good approach to increase the chance of successful asteroseismology with only TESS data, but does not guarantee that the true period spacing pattern can be extracted. To ensure a like-for-like comparison in data analysis methods, as well as forward asteroseismic modelling methodology, we reanalysed the *Kepler* light curves of the best three SPB stars in our sample using our new light-curve extracted method. The fact that the results are extremely similar to our TESS results for the same stars show that much of the scatter between different studies may arise from differences in analysis methodology. In conclusion, our work demonstrates that individual and careful analysis of g-mode pulsators is critical for reliable asteroseismology inference, since the potential data and methodological biases are highly star dependent when using only TESS data.

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DATA AVAILABILITY

This research made use of the following open-access software packages: LIGHTKURVE (<https://lightkurve.github.io/lightkurve/>), a Python package for *Kepler* and TESS data analysis (Lightkurve Collaboration et al. 2018), PERIOD04 (<https://www.period04.net>) for frequency analysis (Lenz & Breger 2005), AMIGO (<https://github.com/TVanReeth/amigo>) for period spacing pattern analysis (Van Reeth et al. 2016, 2018, 2022), as well as astropy (Astropy Collaboration et al. 2022), matplotlib (Hunter 2007) and numpy (Oliphant 2006; van der Walt et al. 2011; Harris et al. 2020).

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APPENDIX A: FREQUENCY EXTRACTION SUMMARY

Tables [A1](#) to [A8](#) list the frequencies extracted from our extracted TESS light curves using PERIOD04 ([Lenz & Breger 2005](#)).

APPENDIX B: AMPLITUDE SPECTRA AND MODELLING FIGURES

Figures showing pre-whitened spectra of the three chunk light curves for all of our stars are listed here. For stars which we then modelled, period spacing patterns with fits from AMIGO and a HRD showing the position of the models with the lowest 50 per cent of MD values are also given. For KIC 4930889 and KIC 7760680, our modelling results are compared to [Pedersen et al. \(2021\)](#) (grey shaded region) and other works.

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Table A1. Extracted frequencies for KIC 3240411. The number of light curve chunks is shown in the first column. The next five columns list the frequency, period, amplitude, phase, and signal to noise ratio of each extracted frequency. The last column(s) mark which frequencies we used to build our period spacing patterns (where possible) and those we judged to be a match with Pedersen et al. (2021). The ‘x-’ mark signifies which frequencies are followed by a gap in the pattern.

no. chunks	f / d^{-1}	P / d	A / mmag	ϕ	S/N	Pedersen pattern
1	0.91420 ± 0.00007	1.09374 ± 0.00008	0.353 ± 0.008	0.44 ± 0.23	7.4	x
2	0.11955 ± 0.00004	8.365 ± 0.003	0.224 ± 0.006	0.57 ± 0.14	5.0	
	0.91421 ± 0.00003	1.09385 ± 0.00003	0.339 ± 0.006	0.76 ± 0.09	7.4	x
	1.18718 ± 0.00006	0.84233 ± 0.00004	0.158 ± 0.006	0.48 ± 0.20	4.8	
	1.23724 ± 0.00005	0.80825 ± 0.00003	0.173 ± 0.006	0.72 ± 0.18	5.7	
	1.51103 ± 0.00007	0.66180 ± 0.00003	0.139 ± 0.006	0.37 ± 0.22	5.0	
	2.7048 ± 0.0001	0.36972 ± 0.00002	0.061 ± 0.006	0.66 ± 0.51	4.6	
3	0.11969 ± 0.00002	8.355 ± 0.001	0.178 ± 0.006	0.079 ± 0.048	5.0	
	0.72156 ± 0.00002	1.38588 ± 0.00004	0.146 ± 0.006	0.519 ± 0.059	5.0	
	0.78973 ± 0.00002	1.26625 ± 0.00003	0.126 ± 0.006	0.346 ± 0.069	4.7	x-
	0.85855 ± 0.00002	1.16476 ± 0.00002	0.158 ± 0.006	0.187 ± 0.055	5.0	x
	0.914893 ± 0.000008	1.09302 ± 0.00001	0.371 ± 0.006	0.396 ± 0.027	10.5	x-
	0.92144 ± 0.00002	1.08525 ± 0.00002	0.156 ± 0.006	0.954 ± 0.064	4.9	
	1.19153 ± 0.00002	0.83926 ± 0.00001	0.193 ± 0.006	0.054 ± 0.057	7.5	x-
	1.19913 ± 0.00002	0.83394 ± 0.00002	0.143 ± 0.006	0.718 ± 0.076	5.7	
	1.23712 ± 0.00001	0.808328 ± 0.000009	0.199 ± 0.006	0.132 ± 0.044	7.3	
	1.45310 ± 0.00002	0.688182 ± 0.000008	0.153 ± 0.006	0.497 ± 0.056	6.4	
	1.51155 ± 0.00002	0.661574 ± 0.000009	0.124 ± 0.006	0.586 ± 0.069	6.1	
	2.70489 ± 0.00004	0.369701 ± 0.000006	0.065 ± 0.006	0.18 ± 0.13	6.3	

Table A2. As Tab. A1 but for KIC 3459297.

no. chunks	f / d^{-1}	P / d	A / mmag	ϕ	SNR	Pedersen pattern
1	0.8390 ± 0.0002	1.1919 ± 0.0003	0.26 ± 0.02	0.8 ± 0.7	5.1	
	0.8726 ± 0.0002	1.1460 ± 0.0002	0.30 ± 0.02	0.8 ± 0.6	5.7	
	0.9065 ± 0.0002	1.1032 ± 0.0003	0.26 ± 0.02	0.6 ± 0.7	4.8	
	0.97910 ± 0.00007	1.02135 ± 0.00007	0.86 ± 0.02	0.4 ± 0.2	8.7	x
	0.98974 ± 0.00003	1.01036 ± 0.00003	2.23 ± 0.02	0.15 ± 0.09	15.2	x-
	1.0347 ± 0.0001	0.9665 ± 0.0001	0.52 ± 0.02	0.9 ± 0.4	7.3	x-
	1.07201 ± 0.00005	0.93283 ± 0.00004	1.13 ± 0.02	0.1 ± 0.2	8.4	x
	1.09220 ± 0.00004	0.91558 ± 0.00003	1.35 ± 0.02	0.8 ± 0.1	16.8	x
2	0.87869 ± 0.00006	1.13805 ± 0.00007	0.29 ± 0.01	0.3 ± 0.2	7.2	
	0.8982 ± 0.0001	1.1134 ± 0.0001	0.17 ± 0.01	0.9 ± 0.3	4.8	
	0.97327 ± 0.00004	1.02746 ± 0.00004	0.45 ± 0.01	1.0 ± 0.1	10.4	x
	0.98962 ± 0.00001	1.01049 ± 0.00001	1.59 ± 0.01	0.53 ± 0.05	22.9	x
	0.99724 ± 0.00005	1.00277 ± 0.00005	0.50 ± 0.01	0.8 ± 0.2	7.6	x-
	1.02687 ± 0.00005	0.97384 ± 0.00005	0.32 ± 0.01	0.6 ± 0.2	8.7	x-
	1.06617 ± 0.00004	0.93793 ± 0.00003	0.47 ± 0.01	0.7 ± 0.1	10.2	x
	1.08540 ± 0.00001	0.92132 ± 0.00001	1.20 ± 0.01	0.80 ± 0.05	21.5	x
	1.10200 ± 0.00004	0.90744 ± 0.00003	0.40 ± 0.01	0.2 ± 0.1	9.7	x
3	0.79885 ± 0.00004	1.25181 ± 0.00006	0.14 ± 0.01	0.9 ± 0.1	4.6	
	0.83489 ± 0.00003	1.19777 ± 0.00004	0.17 ± 0.01	0.4 ± 0.1	5.4	
	0.87856 ± 0.00002	1.13823 ± 0.00002	0.31 ± 0.01	0.82 ± 0.05	8.9	
	0.89830 ± 0.00003	1.11321 ± 0.00004	0.15 ± 0.01	0.6 ± 0.1	5.1	x-
	0.94204 ± 0.00003	1.06152 ± 0.00004	0.17 ± 0.01	0.4 ± 0.1	5.1	x
	0.95814 ± 0.00002	1.04369 ± 0.00002	0.24 ± 0.01	0.02 ± 0.07	6.3	x-
	0.972928 ± 0.000008	1.027825 ± 0.000008	0.67 ± 0.01	0.20 ± 0.03	14.4	x
	0.989974 ± 0.000003	1.010128 ± 0.000003	1.80 ± 0.01	0.314 ± 0.009	27.8	x-
	1.03212 ± 0.00001	0.96888 ± 0.00001	0.35 ± 0.01	0.03 ± 0.05	10.4	x-
	1.06603 ± 0.00001	0.93806 ± 0.00001	0.47 ± 0.01	0.16 ± 0.04	12.5	x
	1.085560 ± 0.000004	0.921184 ± 0.000003	1.28 ± 0.01	0.23 ± 0.01	25.3	x
	1.10687 ± 0.00001	0.90345 ± 0.00001	0.36 ± 0.01	0.95 ± 0.05	9.9	x

Table A3. As Tab. A1 but for KIC 4930889.

no. chunks	f / d^{-1}	P / d	A / mmag	ϕ	SNR	our pattern	Pedersen pattern
1	1.09023 ± 0.00005	0.91723 ± 0.00004	0.98 ± 0.02	0.92 ± 0.17	4.6		x
	1.11011 ± 0.00002	0.90081 ± 0.00002	2.05 ± 0.02	0.628 ± 0.084	10.7		x-
	1.17911 ± 0.00003	0.84810 ± 0.00002	1.45 ± 0.02	0.75 ± 0.12	8.4		x-
	1.213214 ± 0.000008	0.824257 ± 0.000005	5.93 ± 0.02	0.166 ± 0.028	19.2		x
	1.238524 ± 0.000006	0.807413 ± 0.000004	7.69 ± 0.02	0.712 ± 0.022	17.4		x
	2.4793 ± 0.0002	0.40334 ± 0.00002	0.32 ± 0.02	0.65 ± 0.53	5.7		
	4.7133 ± 0.0007	0.21217 ± 0.00003	0.07 ± 0.02	0.2 ± 2.4	4.6		
	4.8027 ± 0.0006	0.2082 ± 0.00003	0.07 ± 0.02	0.2 ± 2.3	5.1		
2	0.02394 ± 0.00002	41.76 ± 0.04	0.68 ± 0.01	0.935 ± 0.074	5.4		
	0.17922 ± 0.00002	5.5797 ± 0.0008	0.61 ± 0.01	0.234 ± 0.084	5.1		
	1.106837 ± 0.000008	0.903476 ± 0.000006	2.00 ± 0.01	0.205 ± 0.026	14.7		x-
	1.13078 ± 0.00003	0.88434 ± 0.00003	0.48 ± 0.01	0.50 ± 0.11	5.2		x-
	1.17239 ± 0.00002	0.85296 ± 0.00001	1.00 ± 0.01	0.566 ± 0.052	9.9		x
	1.19469 ± 0.00001	0.837039 ± 0.000008	1.31 ± 0.01	0.606 ± 0.040	12.0		x
	1.216317 ± 0.000003	0.822154 ± 0.000002	4.85 ± 0.01	0.200 ± 0.011	26.6		x
	1.239863 ± 0.000002	0.806541 ± 0.000002	6.21 ± 0.01	0.9802 ± 0.0084	25.6		x
	1.29455 ± 0.00004	0.77247 ± 0.00002	0.39 ± 0.01	0.62 ± 0.13	4.7		x
	1.71767 ± 0.00004	0.58218 ± 0.00001	0.40 ± 0.01	0.26 ± 0.13	4.8		
	2.34664 ± 0.00009	0.42614 ± 0.00002	0.17 ± 0.01	0.60 ± 0.31	5.7		
	2.45624 ± 0.00009	0.407126 ± 0.00002	0.16 ± 0.01	0.38 ± 0.32	6.0		
	2.47968 ± 0.00006	0.403278 ± 0.000009	0.27 ± 0.01	0.25 ± 0.19	9.3		
	4.7126 ± 0.0003	0.21220 ± 0.00001	0.05 ± 0.01	0.42 ± 0.96	5.5		
	3	0.17912 ± 0.00001	5.5826 ± 0.0003	0.62 ± 0.01	0.563 ± 0.032	6.1	
0.24938 ± 0.00001		4.0099 ± 0.0002	0.44 ± 0.01	0.827 ± 0.045	4.7		
0.99617 ± 0.00002		1.00385 ± 0.00002	0.33 ± 0.01	0.574 ± 0.060	4.8		
1.06810 ± 0.00001		0.93624 ± 0.00001	0.55 ± 0.01	0.413 ± 0.037	6.9	x	x-
1.08899 ± 0.00002		0.91828 ± 0.00001	0.41 ± 0.01	0.317 ± 0.049	5.8	x	x
1.106962 ± 0.000003		0.903374 ± 0.000003	1.98 ± 0.01	0.773 ± 0.010	19.0	x	x-
1.12599 ± 0.00001		0.88811 ± 0.00001	0.49 ± 0.01	0.423 ± 0.041	6.4	x	x
1.15923 ± 0.00002		0.86264 ± 0.00001	0.37 ± 0.01	0.992 ± 0.056	5.3	x	x
1.172867 ± 0.000008		0.852612 ± 0.000005	0.87 ± 0.01	0.916 ± 0.024	11.5	x	x
1.194654 ± 0.000005		0.837063 ± 0.000004	1.25 ± 0.01	0.727 ± 0.016	14.3	x	x
1.216326 ± 0.000001		0.822148 ± 0.000001	4.76 ± 0.01	0.1649 ± 0.0042	32.6	x	x
1.239875 ± 0.000001		0.806533 ± 0.000001	6.16 ± 0.01	0.9368 ± 0.0033	32.3	x	x-
1.26748 ± 0.00002		0.78896 ± 0.00001	0.34 ± 0.01	0.660 ± 0.061	5.3	x	
1.29545 ± 0.00002		0.77193 ± 0.00001	0.27 ± 0.01	0.515 ± 0.076	4.6	x	x-
1.37272 ± 0.00002		0.72848 ± 0.00001	0.30 ± 0.01	0.663 ± 0.065	5.3		x
1.71773 ± 0.00002		0.582168 ± 0.000005	0.42 ± 0.01	0.087 ± 0.048	6.6		
2.32206 ± 0.00005		0.430652 ± 0.000009	0.12 ± 0.01	0.56 ± 0.17	5.7		
2.34685 ± 0.00003		0.426102 ± 0.000006	0.18 ± 0.01	0.87 ± 0.11	7.8		
2.45627 ± 0.00004		0.407121 ± 0.000006	0.16 ± 0.01	0.27 ± 0.13	7.6		
2.47975 ± 0.00002		0.403267 ± 0.000004	0.26 ± 0.01	0.007 ± 0.079	11.4		
4.5841 ± 0.0002		0.218145 ± 0.000007	0.04 ± 0.01	0.22 ± 0.50	5.2		
4.7130 ± 0.0001		0.212177 ± 0.000006	0.05 ± 0.01	0.91 ± 0.42	6.4		
4.8044 ± 0.0001		0.208144 ± 0.000006	0.04 ± 0.01	0.25 ± 0.48	5.6		
4.9954 ± 0.0002	0.200184 ± 0.000008	0.03 ± 0.01	1.00 ± 0.63	4.8			
5.0913 ± 0.0002	0.196415 ± 0.000007	0.03 ± 0.01	0.07 ± 0.58	5.1			

Table A4. As Tab. A1 but for KIC 5941844.

no. chunks	f / d^{-1}	P / d	A / mmag	ϕ	SNR	our pattern	Pedersen pattern
1	0.76769 ± 0.00002	1.30261 ± 0.00004	1.91 ± 0.01	0.35 ± 0.08	8.5		
	0.89986 ± 0.00003	1.11128 ± 0.00003	1.64 ± 0.01	0.66 ± 0.09	8.6		
	1.179536 ± 0.000007	0.847791 ± 0.000005	5.83 ± 0.01	0.88 ± 0.03	13.1		x
	1.21144 ± 0.00002	0.82547 ± 0.00001	2.40 ± 0.01	0.90 ± 0.06	8.1		x-
	1.28714 ± 0.00004	0.77692 ± 0.00002	1.14 ± 0.01	0.6 ± 0.1	6.9		
	1.309107 ± 0.000004	0.763879 ± 0.000002	10.70 ± 0.01	0.09 ± 0.01	17.1		x-
	1.43633 ± 0.00001	0.696220 ± 0.000007	2.93 ± 0.01	0.07 ± 0.05	9.6		x-
	1.72008 ± 0.00002	0.581369 ± 0.000007	1.99 ± 0.01	0.76 ± 0.08	9.5		x
2	0.768667 ± 0.000004	1.300953 ± 0.000006	1.89 ± 0.02	0.91 ± 0.01	11.5		
	0.900248 ± 0.000005	1.110805 ± 0.000006	1.53 ± 0.02	0.29 ± 0.01	11.1		
	0.99675 ± 0.00001	1.00326 ± 0.00001	0.55 ± 0.02	0.47 ± 0.04	4.8		
	1.179178 ± 0.000001	0.8480485 ± 0.0000009	6.01 ± 0.02	0.133 ± 0.004	19.9		x
	1.209829 ± 0.000003	0.826563 ± 0.000002	2.64 ± 0.02	0.541 ± 0.009	14.0		x-
	1.282749 ± 0.000008	0.779576 ± 0.000005	0.87 ± 0.02	0.99 ± 0.03	8.2		
	1.3093818 ± 0.0000007	0.7637192 ± 0.0000004	10.84 ± 0.02	0.128 ± 0.002	24.3		x-
	1.436480 ± 0.000002	0.696146 ± 0.000001	3.00 ± 0.02	0.536 ± 0.008	14.1		x-
	1.60952 ± 0.00002	0.621301 ± 0.000006	0.47 ± 0.02	0.96 ± 0.05	5.6		x
	1.719906 ± 0.000004	0.581427 ± 0.000001	2.01 ± 0.02	0.36 ± 0.01	13.8		x
	2.35836 ± 0.00004	0.424024 ± 0.000007	0.18 ± 0.02	0.0 ± 0.1	5.2		
	2.89913 ± 0.00006	0.344931 ± 0.000007	0.13 ± 0.02	0.1 ± 0.2	6.8		
	4.9771 ± 0.0002	0.200919 ± 0.000006	0.05 ± 0.02	0.6 ± 0.5	5.6		
3	0.610851 ± 0.000009	1.63706 ± 0.00002	0.49 ± 0.01	0.98 ± 0.03	4.9		
	0.768659 ± 0.000002	1.300966 ± 0.000004	1.84 ± 0.01	0.940 ± 0.007	13.9		
	0.898882 ± 0.000003	1.112493 ± 0.000004	1.42 ± 0.01	0.084 ± 0.009	13.0		
	0.995506 ± 0.000009	1.004514 ± 0.000009	0.50 ± 0.01	0.90 ± 0.03	5.9		x
	1.025983 ± 0.000008	0.974675 ± 0.000008	0.55 ± 0.01	0.29 ± 0.02	5.8		x-
	1.1791824 ± 0.0000008	0.8480452 ± 0.0000005	6.06 ± 0.01	0.118 ± 0.002	25.9	x	x
	1.209863 ± 0.000002	0.826540 ± 0.000001	2.53 ± 0.01	0.430 ± 0.005	16.9		x-
	1.278679 ± 0.000005	0.782057 ± 0.000003	0.86 ± 0.01	0.28 ± 0.02	10.3		
	1.3093821 ± 0.0000004	0.7637190 ± 0.0000002	10.66 ± 0.01	0.127 ± 0.001	29.4	x	x-
	1.436474 ± 0.000002	0.6961493 ± 0.0000007	2.94 ± 0.01	0.558 ± 0.004	17.8	x	x-
	1.58965 ± 0.00001	0.629067 ± 0.000004	0.41 ± 0.01	0.50 ± 0.03	6.0		
	1.60809 ± 0.00001	0.621856 ± 0.000005	0.38 ± 0.01	0.99 ± 0.03	5.9		x
	1.719904 ± 0.000002	0.5814279 ± 0.0000008	1.99 ± 0.01	0.364 ± 0.007	17.3	x	x
	2.35836 ± 0.00003	0.424024 ± 0.000004	0.18 ± 0.01	0.01 ± 0.07	6.7		
	2.89907 ± 0.00004	0.344939 ± 0.000004	0.12 ± 0.01	0.3 ± 0.1	7.9		
4.9772 ± 0.0001	0.200918 ± 0.000004	0.04 ± 0.01	0.4 ± 0.3	5.6			

Table A5. As Tab. A1 but for KIC 6352430.

no. chunks	f / d^{-1}	P / d	A / mmag	ϕ	SNR	Pedersen pattern	
1	0.46540 ± 0.00005	2.1487 ± 0.0002	0.444 ± 0.008	0.0 ± 0.2	5.2		
	1.28493 ± 0.00004	0.77825 ± 0.00002	0.556 ± 0.008	0.9 ± 0.1	6.8	x-	
	1.361874 ± 0.000004	0.734282 ± 0.000002	5.548 ± 0.008	0.47 ± 0.01	28.2	x-	
	1.46384 ± 0.00001	0.683136 ± 0.000005	2.015 ± 0.008	0.81 ± 0.04	19.8	x	
	1.518950 ± 0.000004	0.658350 ± 0.000002	5.623 ± 0.008	0.44 ± 0.01	20.2	x	
	1.95435 ± 0.00006	0.51168 ± 0.00002	0.350 ± 0.008	0.9 ± 0.2	5.4		
	2.88100 ± 0.00009	0.34710 ± 0.00001	0.240 ± 0.008	0.7 ± 0.3	7.9		
	2.98302 ± 0.00005	0.335231 ± 0.000006	0.443 ± 0.008	0.9 ± 0.2	13.3		
	3.0868 ± 0.0001	0.32396 ± 0.00001	0.179 ± 0.008	0.4 ± 0.4	8.5		
	3.2467 ± 0.0002	0.30801 ± 0.00002	0.099 ± 0.008	0.3 ± 0.8	5.9		
	3.82240 ± 0.00009	0.261616 ± 0.000006	0.234 ± 0.008	0.8 ± 0.3	13.9		
	5.7136 ± 0.0002	0.175022 ± 0.000008	0.090 ± 0.008	0.7 ± 0.9	12.0		
	5.8150 ± 0.0006	0.17197 ± 0.00002	0.035 ± 0.008	1 ± 2	5.4		
	2	0.40773 ± 0.00002	2.4526 ± 0.0002	0.300 ± 0.005	0.74 ± 0.09	5.1	
		0.46491 ± 0.00002	2.15095 ± 0.00008	0.430 ± 0.005	0.75 ± 0.06	6.8	
0.99781 ± 0.00003		1.00219 ± 0.00003	0.253 ± 0.005	0.8 ± 0.1	4.6	x-	
1.04831 ± 0.00003		0.95392 ± 0.00003	0.251 ± 0.005	0.2 ± 0.1	5.0	x-	
1.12833 ± 0.00004		0.88626 ± 0.00003	0.205 ± 0.005	0.9 ± 0.1	4.8	x	
1.15193 ± 0.00003		0.86811 ± 0.00002	0.281 ± 0.005	0.71 ± 0.09	5.5	x-	
1.25368 ± 0.00003		0.79765 ± 0.00002	0.233 ± 0.005	0.6 ± 0.1	5.2	x	
1.28442 ± 0.00001		0.778561 ± 0.000008	0.562 ± 0.005	0.69 ± 0.05	17.1	x-	
1.361903 ± 0.000001		0.7342668 ± 0.0000007	5.482 ± 0.005	0.365 ± 0.005	37.1	x	
1.464016 ± 0.000004		0.683053 ± 0.000002	1.962 ± 0.005	0.18 ± 0.01	26.0	x	
1.518883 ± 0.000001		0.6583784 ± 0.0000006	5.526 ± 0.005	0.678 ± 0.005	27.4	x	
1.59111 ± 0.00003		0.62849 ± 0.00001	0.265 ± 0.005	0.2 ± 0.1	5.4	x	
1.62115 ± 0.00003		0.61685 ± 0.00001	0.218 ± 0.005	0.9 ± 0.1	5.4		
1.83037 ± 0.00003		0.54634 ± 0.00001	0.236 ± 0.005	0.1 ± 0.1	5.6		
1.95336 ± 0.00002		0.511938 ± 0.000005	0.388 ± 0.005	0.38 ± 0.07	8.0		
2.09541 ± 0.00004		0.477233 ± 0.000009	0.198 ± 0.005	0.3 ± 0.1	5.9		
2.88081 ± 0.00003		0.347124 ± 0.000004	0.235 ± 0.005	0.3 ± 0.1	10.4		
2.98290 ± 0.00002		0.335244 ± 0.000002	0.428 ± 0.005	0.30 ± 0.06	17.1		
3.08649 ± 0.00004		0.323993 ± 0.000005	0.171 ± 0.005	0.6 ± 0.2	12.4		
3.24699 ± 0.00007		0.307978 ± 0.000006	0.111 ± 0.005	0.2 ± 0.2	10.2		
3.82216 ± 0.00003		0.261632 ± 0.000002	0.236 ± 0.005	0.6 ± 0.1	19.6		
5.71317 ± 0.00009	0.175034 ± 0.000003	0.084 ± 0.005	0.1 ± 0.3	15.6			
5.8158 ± 0.0002	0.171945 ± 0.000007	0.032 ± 0.005	0.0 ± 0.8	6.8			
3	0.15328 ± 0.00002	6.5241 ± 0.0007	0.172 ± 0.006	0.78 ± 0.06	4.8		
	0.40774 ± 0.00001	2.45254 ± 0.00006	0.298 ± 0.006	0.71 ± 0.03	6.4		
	0.464781 ± 0.000007	2.15155 ± 0.00003	0.446 ± 0.006	0.20 ± 0.02	9.0		
	0.99783 ± 0.00001	1.00218 ± 0.00001	0.286 ± 0.006	0.76 ± 0.03	6.4	x-	
	1.04827 ± 0.00001	0.95395 ± 0.00001	0.236 ± 0.006	0.32 ± 0.04	5.7	x-	
	1.12858 ± 0.00001	0.88607 ± 0.00001	0.216 ± 0.006	0.00 ± 0.04	5.6	x	
	1.15207 ± 0.00002	0.86801 ± 0.00001	0.197 ± 0.006	0.25 ± 0.05	5.3	x-	
	1.25385 ± 0.00002	0.79754 ± 0.00001	0.173 ± 0.006	0.04 ± 0.06	4.9	x	
	1.284457 ± 0.000006	0.778539 ± 0.000003	0.546 ± 0.006	0.56 ± 0.02	11.1	x-	
	1.3619183 ± 0.0000005	0.7342584 ± 0.0000003	5.624 ± 0.006	0.308 ± 0.002	46.6	x-	
	1.464013 ± 0.000002	0.6830542 ± 0.0000007	1.998 ± 0.006	0.189 ± 0.005	32.6	x	
	1.5188819 ± 0.0000005	0.6583790 ± 0.0000002	5.660 ± 0.006	0.679 ± 0.002	34.1	x	
	1.59108 ± 0.00001	0.628502 ± 0.000005	0.261 ± 0.006	0.33 ± 0.04	6.2	x-	
	1.62103 ± 0.00001	0.616893 ± 0.000005	0.230 ± 0.006	0.36 ± 0.04	6.1		
	1.75471 ± 0.00002	0.569894 ± 0.000007	0.141 ± 0.006	0.34 ± 0.07	4.8	x	
	1.81780 ± 0.00002	0.550115 ± 0.000006	0.158 ± 0.006	0.74 ± 0.06	5.1		
	1.82978 ± 0.00001	0.546515 ± 0.000004	0.200 ± 0.006	0.19 ± 0.05	5.6		
	1.95276 ± 0.00002	0.512097 ± 0.000004	0.246 ± 0.007	0.41 ± 0.05	7.5		
	1.95906 ± 0.00002	0.510449 ± 0.000004	0.219 ± 0.007	0.40 ± 0.06	6.2		
	2.10129 ± 0.00002	0.475899 ± 0.000004	0.170 ± 0.006	0.70 ± 0.06	5.9		
	2.17571 ± 0.00002	0.459621 ± 0.000004	0.162 ± 0.006	0.42 ± 0.06	6.5		
	2.88081 ± 0.00001	0.347125 ± 0.000002	0.231 ± 0.006	0.35 ± 0.04	13.5		
	2.982919 ± 0.000007	0.3352421 ± 0.0000008	0.441 ± 0.006	0.23 ± 0.02	21.8		
	3.08637 ± 0.00002	0.324006 ± 0.000002	0.169 ± 0.006	0.99 ± 0.06	14.5		
	3.24693 ± 0.00003	0.307983 ± 0.000002	0.117 ± 0.006	0.42 ± 0.08	13.6		
	3.82215 ± 0.00001	0.2616328 ± 0.0000009	0.237 ± 0.006	0.63 ± 0.04	21.3		
	5.71326 ± 0.00003	0.175032 ± 0.000001	0.086 ± 0.006	0.7 ± 0.1	18.8		
5.8163 ± 0.0001	0.171931 ± 0.000004	0.025 ± 0.006	0.4 ± 0.4	6.2			

Table A6. As Tab. A1 but for KIC 7760680.

no. chunks	f / d^{-1}	P / d	A / mmag	ϕ	SNR	our pattern	Pedersen pattern
1	0.81185 ± 0.00001	1.23175 ± 0.00002	2.07 ± 0.01	0.46 ± 0.05	11.2		x-
	0.838727 ± 0.000006	1.192283 ± 0.000008	5.16 ± 0.01	0.51 ± 0.02	17.1		x-
	0.861832 ± 0.000004	1.160319 ± 0.000005	7.89 ± 0.01	0.32 ± 0.01	18.3		x-
	0.88909 ± 0.00001	1.12474 ± 0.00002	2.13 ± 0.01	0.15 ± 0.05	12.1		x-
	0.90737 ± 0.00002	1.10209 ± 0.00003	1.27 ± 0.01	0.64 ± 0.08	7.7		
	0.96657 ± 0.00005	1.03459 ± 0.00005	0.61 ± 0.01	0.7 ± 0.2	7.5		x
	0.99341 ± 0.00003	1.00663 ± 0.00003	0.90 ± 0.01	0.3 ± 0.1	9.3		x
	1.7267 ± 0.0002	0.57914 ± 0.00005	0.19 ± 0.01	0.2 ± 0.5	5.4		
	1.7674 ± 0.0002	0.56580 ± 0.00006	0.16 ± 0.01	0.6 ± 0.6	4.9		
	1.8067 ± 0.0001	0.55351 ± 0.00004	0.23 ± 0.01	0.7 ± 0.4	6.7		
2	0.79953 ± 0.00002	1.25074 ± 0.00004	0.492 ± 0.009	0.78 ± 0.09	5.0	x	x-
	0.808658 ± 0.000008	1.23662 ± 0.00001	1.624 ± 0.009	0.78 ± 0.03	14.1	x	
	0.82522 ± 0.00002	1.21179 ± 0.00002	0.771 ± 0.008	0.13 ± 0.06	9.1	x	x
	0.838492 ± 0.000004	1.192618 ± 0.000005	5.12 ± 0.01	0.34 ± 0.01	25.3	x	x
	0.84687 ± 0.00002	1.18082 ± 0.00003	0.85 ± 0.01	0.18 ± 0.07	8.0	x	x
	0.862788 ± 0.000002	1.159033 ± 0.000002	6.98 ± 0.01	0.942 ± 0.006	27.3	x	x
	0.87476 ± 0.00001	1.14317 ± 0.00002	0.965 ± 0.009	0.72 ± 0.04	9.0	x	x
	0.895063 ± 0.000004	1.117240 ± 0.000006	2.359 ± 0.007	0.08 ± 0.02	17.8	x	
	0.91726 ± 0.00001	1.09021 ± 0.00002	0.784 ± 0.007	0.69 ± 0.05	9.7	x	x-
	0.94197 ± 0.00003	1.06161 ± 0.00004	0.323 ± 0.007	0.2 ± 0.1	5.0	x	
	0.96858 ± 0.00002	1.03244 ± 0.00002	0.619 ± 0.007	0.58 ± 0.06	8.6	x	x
	0.99229 ± 0.00001	1.00777 ± 0.00001	1.039 ± 0.007	0.23 ± 0.03	11.0	x	x
	1.01917 ± 0.00003	0.98119 ± 0.00003	0.300 ± 0.007	0.3 ± 0.1	5.2	x	x
	1.72568 ± 0.00005	0.57948 ± 0.00002	0.188 ± 0.007	0.8 ± 0.2	5.6		
	1.80844 ± 0.00004	0.55296 ± 0.00001	0.253 ± 0.007	0.4 ± 0.1	8.5		
3	0.73347 ± 0.00002	1.36337 ± 0.00003	0.211 ± 0.008	0.12 ± 0.06	4.7		x-
	0.802202 ± 0.000008	1.24657 ± 0.00001	0.513 ± 0.008	0.49 ± 0.03	7.8	x	x
	0.814190 ± 0.000003	1.228214 ± 0.000004	1.481 ± 0.008	0.211 ± 0.009	17.6	x	x
	0.82674 ± 0.00001	1.20958 ± 0.00001	0.484 ± 0.009	0.87 ± 0.03	7.5	x	x
	0.838501 ± 0.000001	1.192604 ± 0.000001	4.520 ± 0.009	0.291 ± 0.003	30.4	x	x
	0.850696 ± 0.000005	1.175509 ± 0.000007	0.841 ± 0.009	0.49 ± 0.02	10.4	x	x
	0.8628516 ± 0.0000007	1.1589478 ± 0.0000009	7.16 ± 0.01	0.723 ± 0.002	33.8	x	x
	0.870148 ± 0.000006	1.149229 ± 0.000008	1.00 ± 0.01	0.04 ± 0.02	8.8	x	x
	0.88238 ± 0.00001	1.13330 ± 0.00002	0.373 ± 0.009	0.31 ± 0.05	6.1		
	0.894832 ± 0.000002	1.117529 ± 0.000003	2.514 ± 0.009	0.868 ± 0.007	22.4	x	x
	0.90272 ± 0.00001	1.10776 ± 0.00001	0.453 ± 0.009	0.15 ± 0.03	6.8		
	0.917512 ± 0.000009	1.08990 ± 0.00001	0.500 ± 0.008	0.86 ± 0.03	11.3	x	x
	0.93198 ± 0.00001	1.07298 ± 0.00001	0.332 ± 0.008	0.51 ± 0.04	6.0	x-	x-
	0.968029 ± 0.000008	1.033027 ± 0.000009	0.489 ± 0.008	0.47 ± 0.03	8.3	x	x
	0.992276 ± 0.000004	1.007784 ± 0.000004	1.020 ± 0.008	0.26 ± 0.01	14.7	x	x
	1.01889 ± 0.00002	0.98146 ± 0.00002	0.219 ± 0.008	0.25 ± 0.06	5.3	x	x
	1.72570 ± 0.00002	0.579474 ± 0.000006	0.200 ± 0.008	0.75 ± 0.06	7.7		
	1.80853 ± 0.00002	0.552937 ± 0.000005	0.226 ± 0.008	0.12 ± 0.05	9.3		

Table A7. As Tab. A1 but for KIC 8766405.

no. chunks	f / d^{-1}	P / d	A / mmag	ϕ	SNR	Pedersen pattern
1	0.03570 ± 0.00006	28.01 ± 0.05	0.235 ± 0.005	0.7 ± 0.2	5.1	
	0.14803 ± 0.00008	6.756 ± 0.004	0.205 ± 0.005	0.5 ± 0.3	4.7	
	0.85166 ± 0.00005	1.17418 ± 0.00006	0.348 ± 0.005	0.1 ± 0.2	7.3	x
	0.86633 ± 0.00001	1.15429 ± 0.00002	1.224 ± 0.005	0.92 ± 0.05	15.6	x
	1.7337 ± 0.0001	0.57682 ± 0.00004	0.121 ± 0.005	0.8 ± 0.5	5.7	
	1.82233 ± 0.00003	0.548749 ± 0.000009	0.550 ± 0.006	0.2 ± 0.1	10.4	
	1.832841 ± 0.000005	0.545601 ± 0.000002	3.024 ± 0.006	0.90 ± 0.02	22.0	
	1.97717 ± 0.00001	0.505773 ± 0.000004	1.050 ± 0.005	0.74 ± 0.05	19.6	
	2.8439 ± 0.0001	0.35163 ± 0.00001	0.161 ± 0.005	0.5 ± 0.3	8.8	
	3.66663 ± 0.00003	0.272730 ± 0.000002	0.507 ± 0.005	0.6 ± 0.1	18.4	
	3.7113 ± 0.0002	0.26945 ± 0.00002	0.068 ± 0.005	0.4 ± 0.8	5.6	
	3.8104 ± 0.0001	0.262437 ± 0.000008	0.129 ± 0.005	0.4 ± 0.4	8.6	
	3.9544 ± 0.0002	0.25288 ± 0.00001	0.069 ± 0.005	0.5 ± 0.8	5.7	
	5.6846 ± 0.0002	0.175914 ± 0.000007	0.067 ± 0.005	0.1 ± 0.8	7.2	
	7.3419 ± 0.0004	0.136204 ± 0.000007	0.042 ± 0.005	1 ± 1	6.2	
	2	0.03543 ± 0.00003	28.22 ± 0.02	0.198 ± 0.004	0.6 ± 0.1	5.2
0.14932 ± 0.00003		6.697 ± 0.002	0.172 ± 0.004	0.9 ± 0.1	5.3	
0.85020 ± 0.00001		1.17619 ± 0.00002	0.459 ± 0.004	0.31 ± 0.04	11.9	x
0.864891 ± 0.000004		1.156214 ± 0.000006	1.385 ± 0.004	0.02 ± 0.01	24.1	x
1.68668 ± 0.00007		0.59288 ± 0.00002	0.086 ± 0.004	0.8 ± 0.2	4.9	
1.73477 ± 0.00004		0.57644 ± 0.00001	0.146 ± 0.004	0.8 ± 0.1	8.1	
1.81740 ± 0.00001		0.550237 ± 0.000004	0.437 ± 0.004	0.66 ± 0.05	18.9	
1.832358 ± 0.000002		0.5457449 ± 0.0000005	3.132 ± 0.004	0.619 ± 0.006	32.4	
1.977166 ± 0.000005		0.505775 ± 0.000001	1.047 ± 0.004	0.76 ± 0.02	28.8	
2.8273 ± 0.0001		0.35370 ± 0.00001	0.059 ± 0.004	0.5 ± 0.3	4.9	
2.84205 ± 0.00003		0.351858 ± 0.000004	0.171 ± 0.004	0.0 ± 0.1	12.0	
3.65176 ± 0.00005		0.273841 ± 0.000004	0.122 ± 0.004	0.7 ± 0.2	11.6	
3.66460 ± 0.00001		0.2728811 ± 0.0000009	0.511 ± 0.004	0.79 ± 0.04	26.8	
3.80962 ± 0.00004		0.262493 ± 0.000003	0.132 ± 0.004	0.3 ± 0.1	11.9	
3.95414 ± 0.00008		0.252899 ± 0.000005	0.069 ± 0.004	0.4 ± 0.3	7.6	
5.4830 ± 0.0001		0.182381 ± 0.000004	0.055 ± 0.004	0.4 ± 0.4	7.7	
5.4970 ± 0.0001		0.181916 ± 0.000005	0.040 ± 0.004	0.4 ± 0.5	6.1	
5.68431 ± 0.00008		0.175923 ± 0.000002	0.074 ± 0.004	0.1 ± 0.3	10.8	
7.3194 ± 0.0003	0.136623 ± 0.000005	0.022 ± 0.004	0.7 ± 0.9	4.7		
7.3380 ± 0.0002	0.136277 ± 0.000003	0.034 ± 0.004	0.6 ± 0.6	6.8		
3	0.03541 ± 0.00001	28.24 ± 0.01	0.170 ± 0.005	0.68 ± 0.05	5.5	
	0.849929 ± 0.000007	1.176568 ± 0.000009	0.395 ± 0.005	0.24 ± 0.02	13.4	x
	0.864966 ± 0.000002	1.156114 ± 0.000003	1.384 ± 0.005	0.757 ± 0.006	29.4	x
	1.72986 ± 0.00002	0.578081 ± 0.000006	0.142 ± 0.005	0.20 ± 0.06	7.9	
	1.817263 ± 0.000005	0.550278 ± 0.000002	0.502 ± 0.005	0.12 ± 0.02	20.4	
	1.8323258 ± 0.0000009	0.5457545 ± 0.0000003	2.957 ± 0.005	0.726 ± 0.003	36.8	
	1.977266 ± 0.000002	0.5057489 ± 0.0000006	1.065 ± 0.005	0.409 ± 0.008	33.9	
	2.84221 ± 0.00002	0.351839 ± 0.000002	0.166 ± 0.005	0.48 ± 0.05	12.1	
	3.664635 ± 0.000007	0.2728785 ± 0.0000005	0.385 ± 0.005	0.66 ± 0.02	27.6	
	3.80962 ± 0.00002	0.262493 ± 0.000001	0.127 ± 0.005	0.26 ± 0.07	12.8	
	3.95460 ± 0.00004	0.252870 ± 0.000002	0.068 ± 0.005	0.8 ± 0.1	7.8	
	5.48307 ± 0.00006	0.182380 ± 0.000002	0.045 ± 0.005	0.2 ± 0.2	8.7	
	5.68447 ± 0.00003	0.175918 ± 0.000001	0.075 ± 0.005	0.5 ± 0.1	13.8	
	7.33776 ± 0.00007	0.136281 ± 0.000001	0.036 ± 0.005	0.5 ± 0.2	9.0	

Table A8. As Tab. A1 but for KIC 11360704.

no. chunks	f / d^{-1}	P / d	A / mmag	ϕ	SNR	Pedersen pattern
1	0.34019 ± 0.00007	2.9395 ± 0.0006	0.39 ± 0.01	0.0 ± 0.3	6.7	
	0.38767 ± 0.00005	2.5795 ± 0.0003	0.60 ± 0.01	0.7 ± 0.2	7.9	
	0.54529 ± 0.00007	1.8339 ± 0.0002	0.42 ± 0.01	0.7 ± 0.2	7.2	
	1.91205 ± 0.00006	0.52300 ± 0.00002	0.51 ± 0.01	0.4 ± 0.2	10.7	
	1.9821 ± 0.0001	0.50452 ± 0.00003	0.23 ± 0.01	0.6 ± 0.5	5.2	
	2.05266 ± 0.00005	0.48717 ± 0.00001	0.56 ± 0.01	0.5 ± 0.2	9.9	
	2.07341 ± 0.00003	0.482297 ± 0.000007	1.04 ± 0.01	0.1 ± 0.1	15.6	x-
	2.46342 ± 0.00003	0.405940 ± 0.000005	1.04 ± 0.01	0.9 ± 0.1	13.3	x
	3.9823 ± 0.0001	0.251113 ± 0.000008	0.22 ± 0.01	0.1 ± 0.5	4.9	
	4.10268 ± 0.00007	0.243743 ± 0.000004	0.40 ± 0.01	0.4 ± 0.3	6.9	
	4.12997 ± 0.00009	0.242133 ± 0.000005	0.33 ± 0.01	0.9 ± 0.3	5.6	
	4.16322 ± 0.00009	0.240199 ± 0.000005	0.33 ± 0.01	0.5 ± 0.3	6.2	
	4.3269 ± 0.0001	0.231110 ± 0.000007	0.24 ± 0.01	0.1 ± 0.4	4.8	
	4.37692 ± 0.00003	0.228471 ± 0.000002	0.96 ± 0.01	0.7 ± 0.1	13.0	
	4.5372 ± 0.0001	0.220401 ± 0.000006	0.24 ± 0.01	0.7 ± 0.4	4.9	
	4.92705 ± 0.00004	0.202961 ± 0.000002	0.68 ± 0.01	0.8 ± 0.2	11.2	
	2	0.34223 ± 0.00003	2.9220 ± 0.0002	0.369 ± 0.007	0.83 ± 0.09	9.2
0.38874 ± 0.00002		2.5724 ± 0.0001	0.558 ± 0.007	0.94 ± 0.06	11.2	
0.54323 ± 0.00002		1.84085 ± 0.00007	0.464 ± 0.007	0.04 ± 0.07	11.3	
1.77814 ± 0.00005		0.56238 ± 0.00002	0.202 ± 0.007	0.9 ± 0.2	6.1	
1.90992 ± 0.00003		0.523581 ± 0.000008	0.354 ± 0.007	0.9 ± 0.1	10.0	
1.98253 ± 0.00004		0.50441 ± 0.00001	0.237 ± 0.007	1.0 ± 0.1	7.0	
2.05669 ± 0.00003		0.486218 ± 0.000006	0.376 ± 0.007	0.22 ± 0.09	7.9	
2.07635 ± 0.00001		0.481613 ± 0.000003	0.781 ± 0.007	0.68 ± 0.04	19.7	x-
2.46345 ± 0.00001		0.405935 ± 0.000002	0.964 ± 0.007	0.79 ± 0.04	20.3	x
3.83033 ± 0.00007		0.261074 ± 0.000005	0.152 ± 0.007	0.8 ± 0.2	5.5	
3.98153 ± 0.00004		0.251160 ± 0.000002	0.282 ± 0.007	0.7 ± 0.1	7.7	
4.00098 ± 0.00006		0.249938 ± 0.000004	0.173 ± 0.007	0.7 ± 0.2	5.4	
4.10259 ± 0.00003		0.243749 ± 0.000002	0.354 ± 0.007	0.7 ± 0.1	8.8	
4.13334 ± 0.00003		0.241935 ± 0.000002	0.330 ± 0.007	0.9 ± 0.1	8.1	
4.16440 ± 0.00004		0.240130 ± 0.000002	0.275 ± 0.007	0.3 ± 0.1	7.7	
4.30554 ± 0.00007		0.232259 ± 0.000004	0.147 ± 0.007	0.6 ± 0.2	5.0	
4.32811 ± 0.00004		0.231048 ± 0.000002	0.246 ± 0.007	1.0 ± 0.1	7.5	
4.36834 ± 0.00003		0.228920 ± 0.000001	0.369 ± 0.007	0.3 ± 0.1	10.2	
4.37874 ± 0.00001		0.2283760 ± 0.0000006	0.922 ± 0.007	0.19 ± 0.04	18.3	
4.38843 ± 0.00004		0.227872 ± 0.000002	0.289 ± 0.007	0.4 ± 0.1	7.6	
4.41419 ± 0.00006	0.226542 ± 0.000003	0.158 ± 0.007	0.1 ± 0.2	5.3		
4.53457 ± 0.00005	0.220528 ± 0.000002	0.204 ± 0.007	0.0 ± 0.2	6.4		
4.92696 ± 0.00002	0.2029650 ± 0.0000006	0.636 ± 0.007	0.16 ± 0.05	15.6		
4.98934 ± 0.00008	0.200427 ± 0.000003	0.132 ± 0.007	0.4 ± 0.3	5.4		
3	0.10239 ± 0.00001	9.767 ± 0.001	0.75 ± 0.02	0.91 ± 0.03	5.4	
	0.34217 ± 0.00001	2.9225 ± 0.0001	0.57 ± 0.02	0.03 ± 0.05	5.1	
	0.389079 ± 0.000001	2.570172 ± 0.000009	32 ± 1	0.898 ± 0.004	10.1	
	0.389101 ± 0.000001	2.57003 ± 0.00001	32 ± 1	0.325 ± 0.004	7.2	
	1.909947 ± 0.000009	0.523575 ± 0.000003	0.90 ± 0.02	0.82 ± 0.03	12.3	
	2.02433 ± 0.00002	0.493990 ± 0.000005	0.41 ± 0.02	0.25 ± 0.06	6.8	
	2.05608 ± 0.00001	0.486362 ± 0.000003	0.81 ± 0.02	0.33 ± 0.03	12.0	x
	2.07140 ± 0.00001	0.482765 ± 0.000002	0.85 ± 0.02	0.26 ± 0.03	11.3	x-
	2.463113 ± 0.000007	0.405990 ± 0.000001	1.14 ± 0.02	0.95 ± 0.02	14.5	x
	4.09748 ± 0.00001	0.2440523 ± 0.0000009	0.58 ± 0.02	0.84 ± 0.05	6.8	
	4.12875 ± 0.00001	0.2422038 ± 0.0000007	0.72 ± 0.02	0.30 ± 0.04	8.0	
	4.15940 ± 0.00001	0.2404192 ± 0.0000009	0.57 ± 0.02	0.11 ± 0.05	7.0	
	4.373041 ± 0.000008	0.2286738 ± 0.0000004	1.05 ± 0.02	0.42 ± 0.03	10.4	
4.92773 ± 0.00001	0.2029332 ± 0.0000005	0.74 ± 0.02	0.47 ± 0.04	8.9		

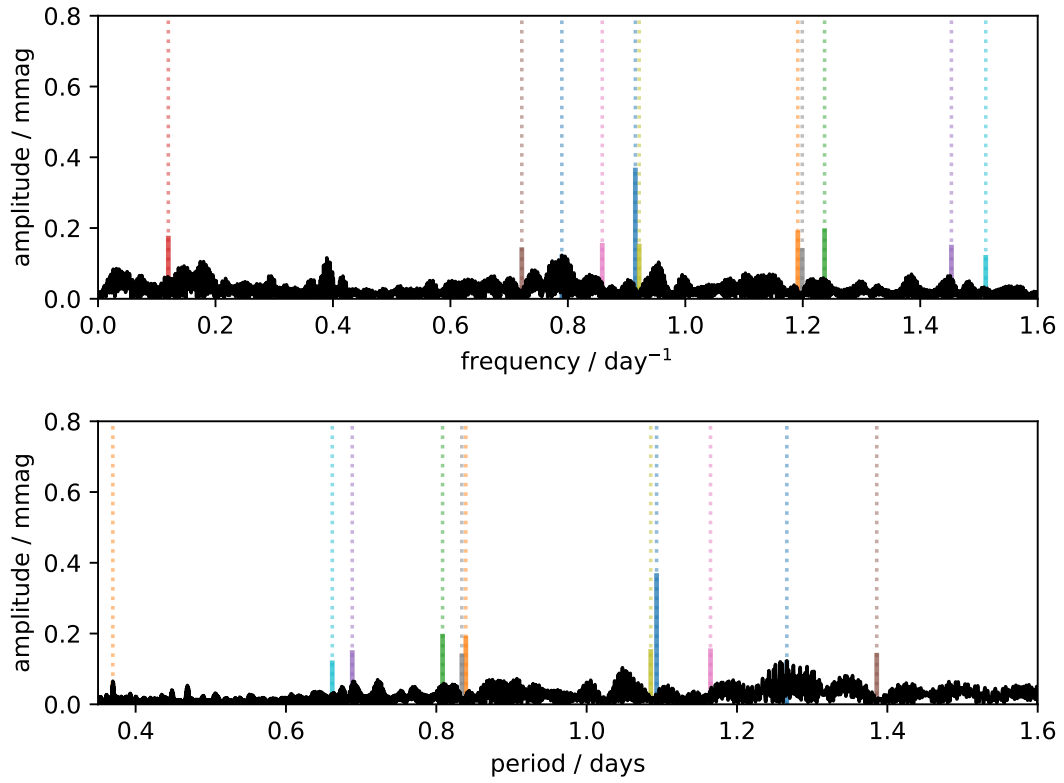


Figure B1. KIC 3240411

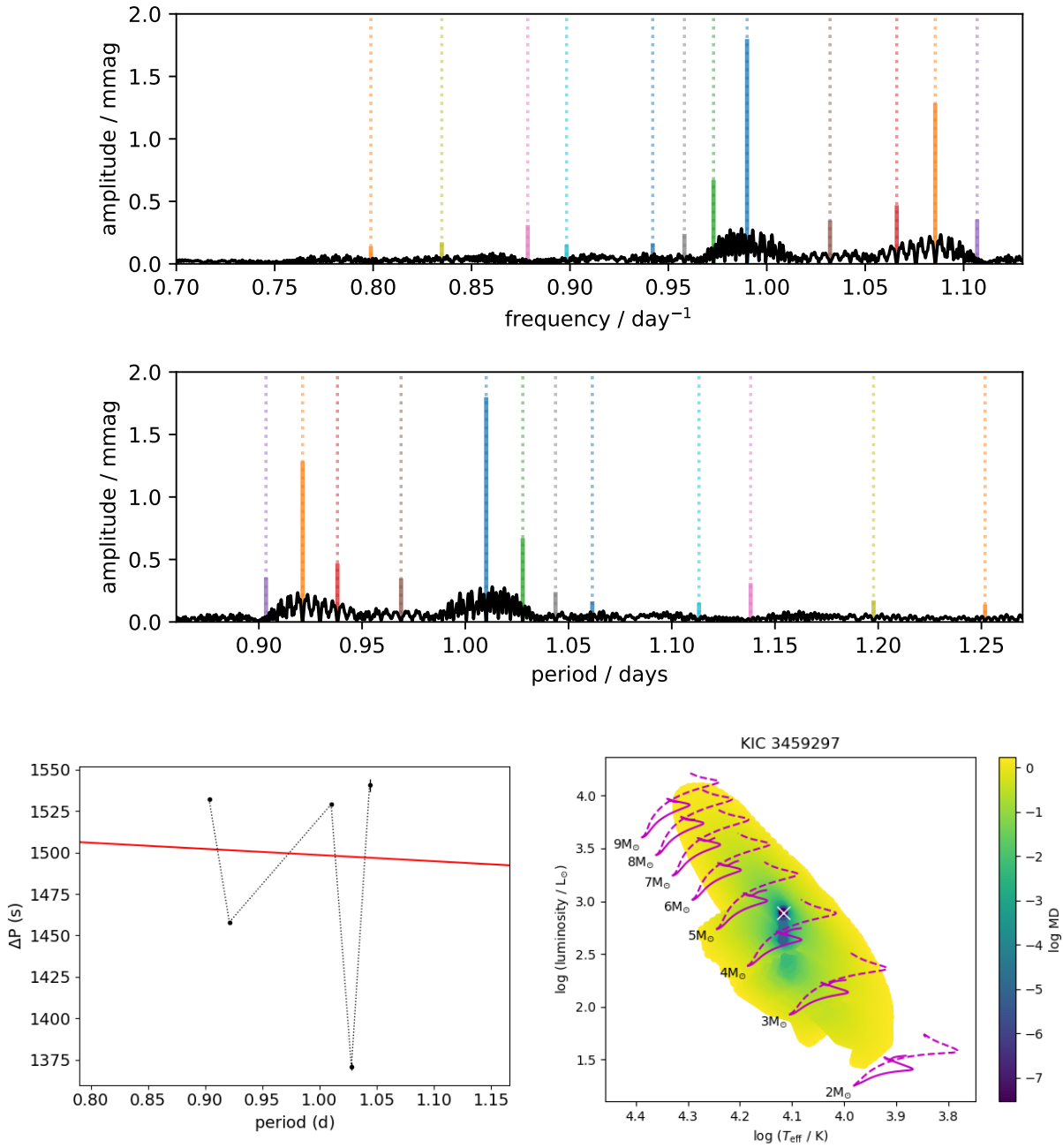


Figure B2. KIC 3459297

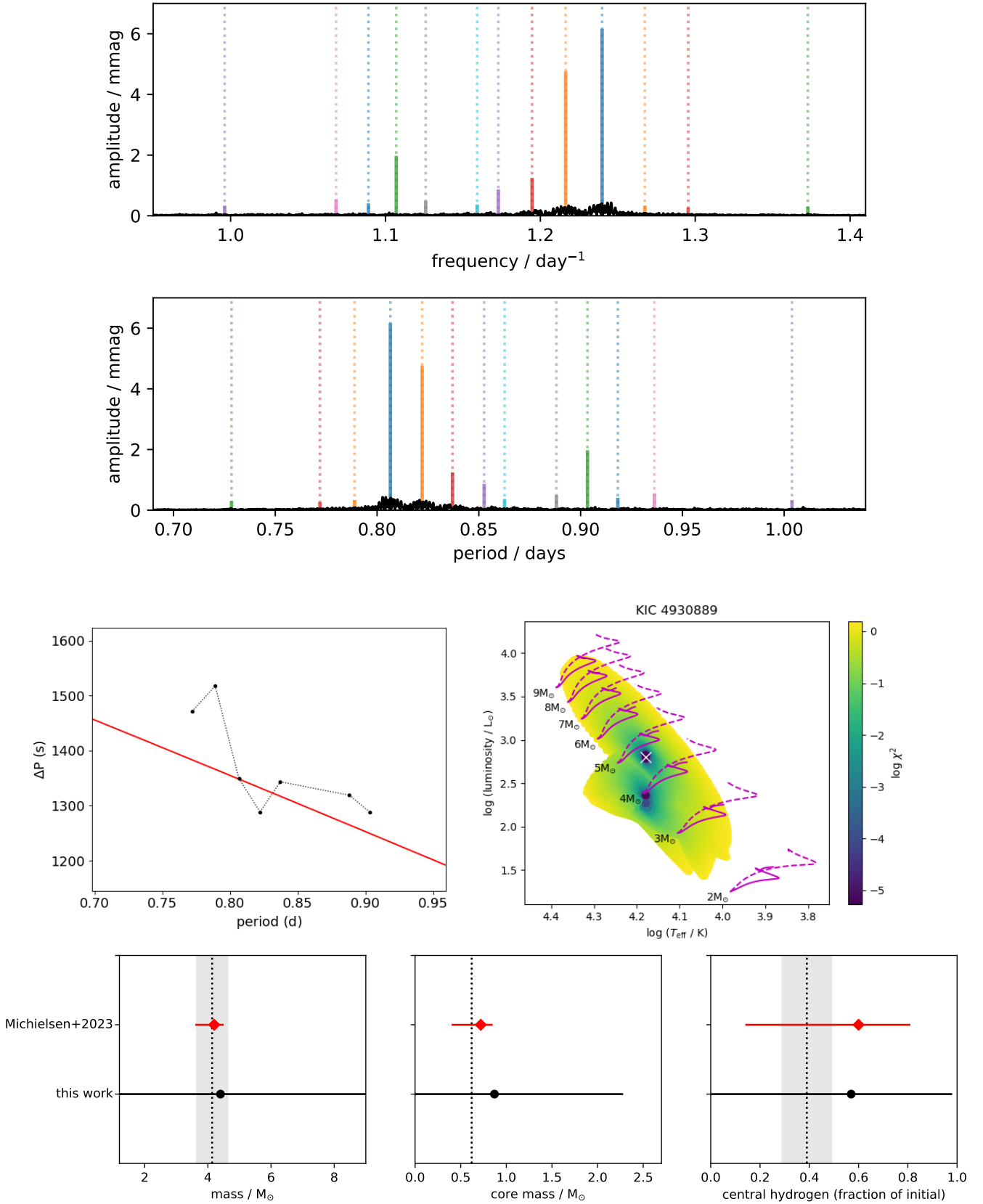


Figure B3. KIC 4930889. Red diamonds plotted on the lower panels come from [Michielsen et al. \(2023\)](#), and correspond to the lowest MD best fit model using period spacings (their Tab. 5).

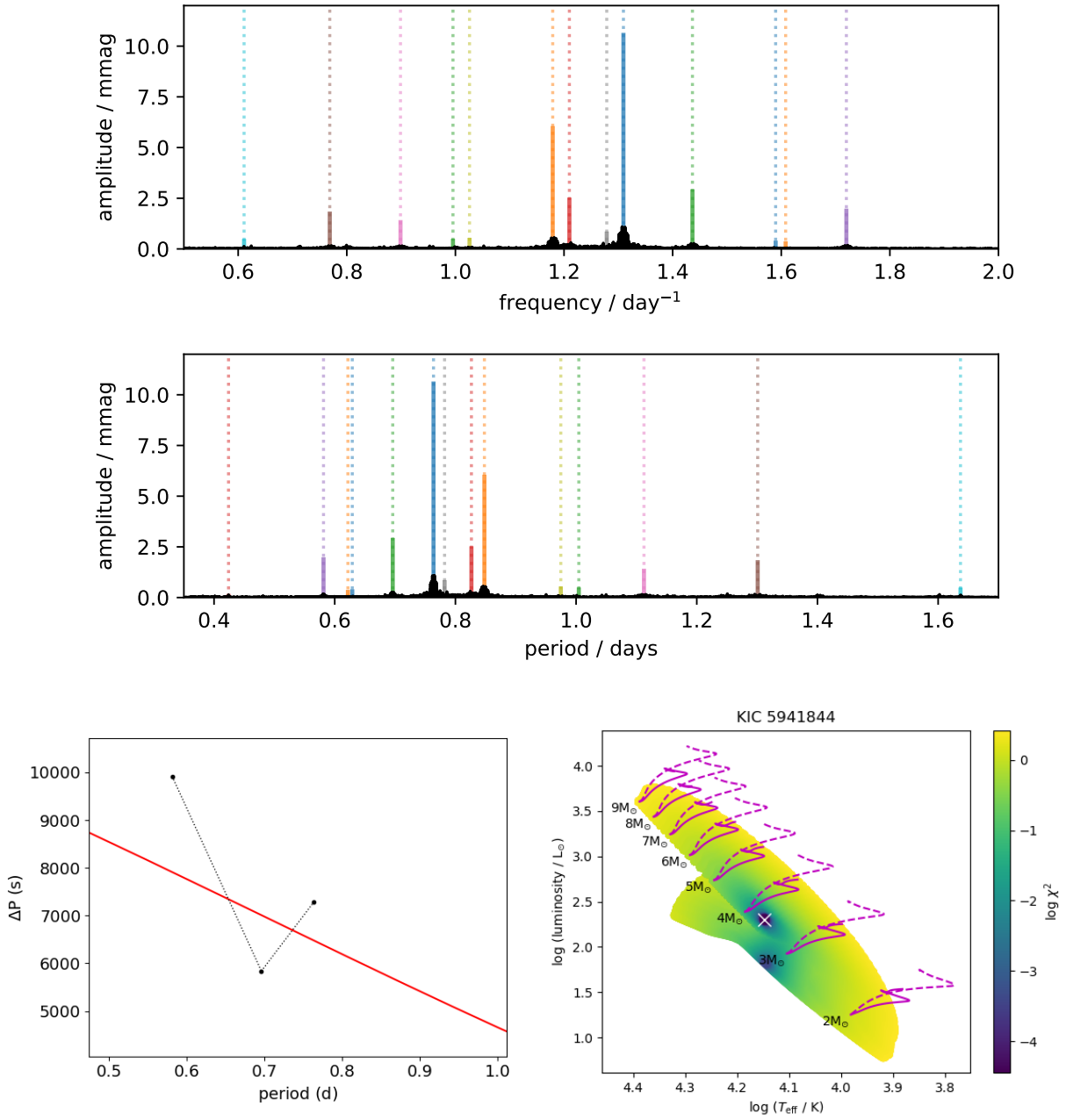


Figure B4. KIC 5941844

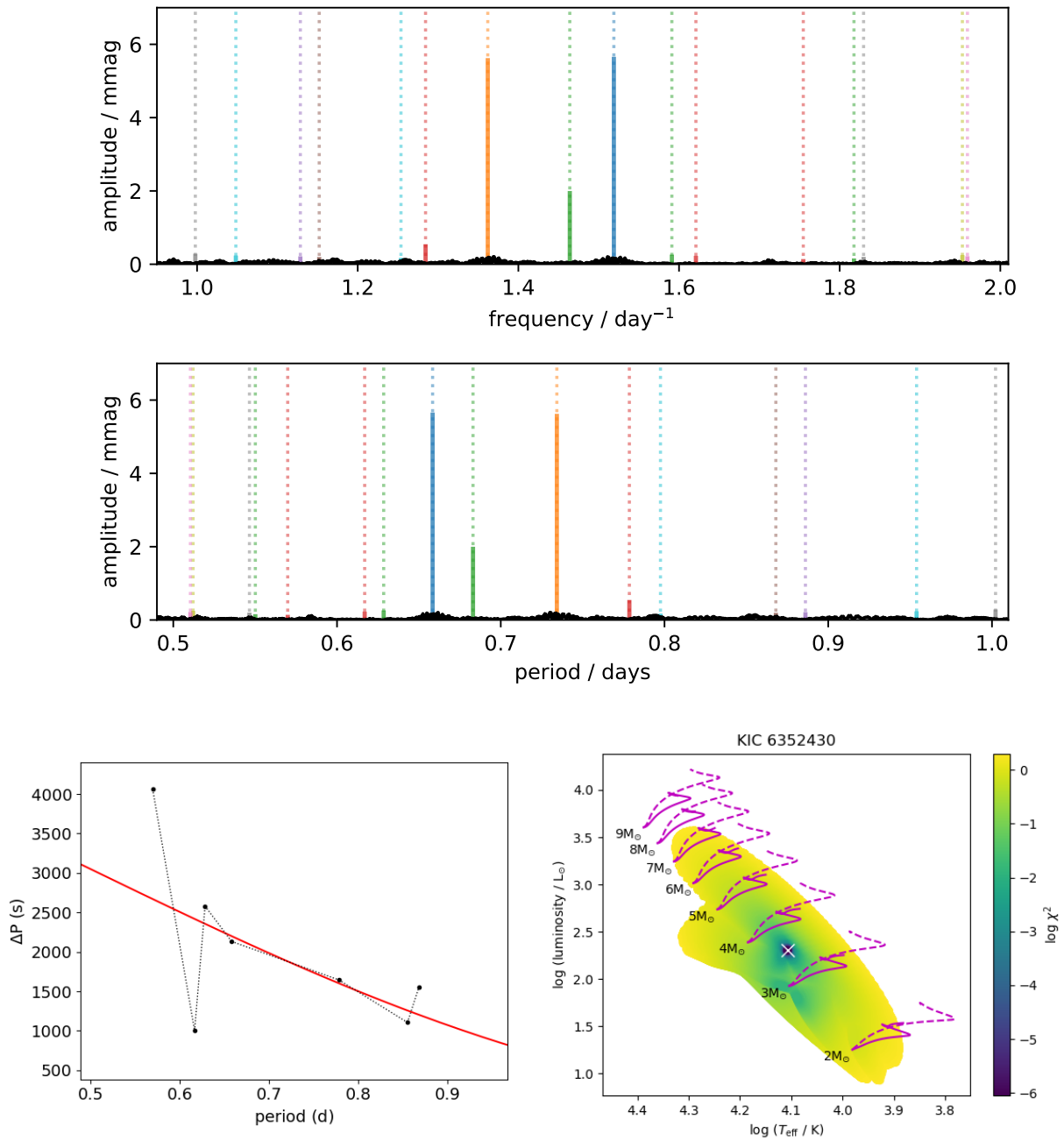


Figure B5. KIC 6352430

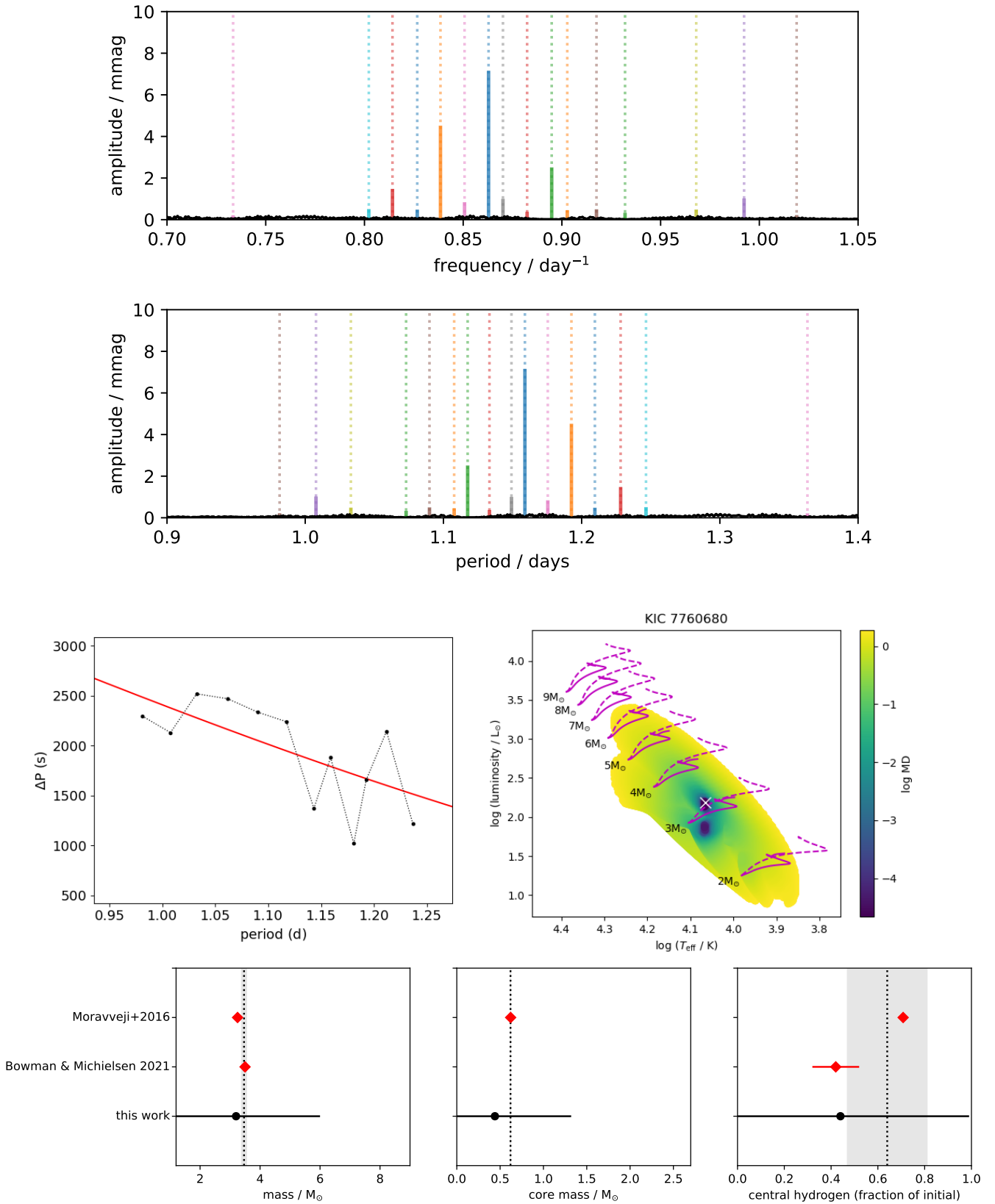


Figure B6. KIC 7760680. Red diamonds in the lower panels are modelling results from Moravveji et al. (2016) and Bowman & Michielsen (2021).

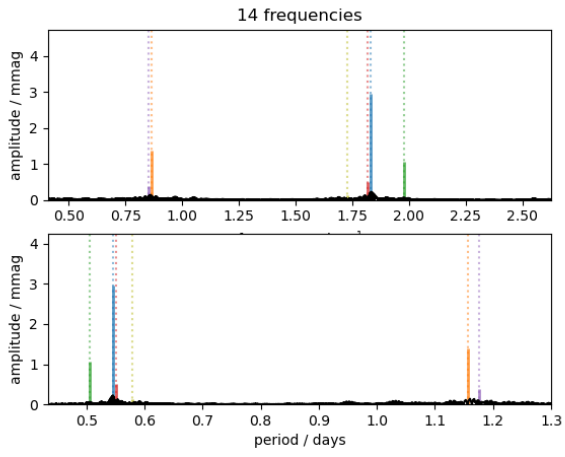


Figure B7. KIC 8766405

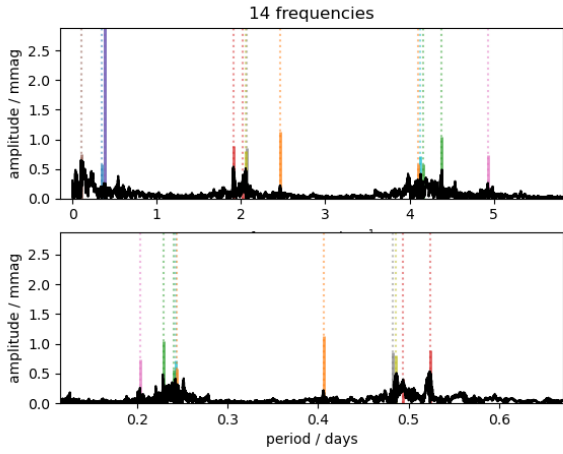


Figure B8. KIC 1136704